

## Answers to

- 1)  $a^2 + 4a - 1$   
 5)  $3n^3 + 5n - 3$   
 9)  $-1$   
 13)  $-3t^3 - 9t^2 + 12t$   
 17)  $-8a^3 - 16a^2 - 8a$   
 20)  $a^3 - 2a^2 - 4a + 8$   
  
 24)  $\frac{x^2}{2}$   
 28)  $\frac{-3n^3 + 5n}{2n + 3}$   
 32)  $28x - 8$   
 36)  $3n^2 - 9n - 18$   
 39)  $-3n$   
 43)  $-3x^3 + x^2 - 4$   
 47)  $9x^2 - 12x + 3$   
 51)  $8n^3 - 36n^2 + 54n - 26$   
 54)  $4n + 6$   
 58)  $-3n^3 - 27n^2 - 81n - 80$   
 61)  $4$   
 65)  $-39$   
 69)  $1$   
  
 73)  $-30$   
 77)  $8$   
 81)  $g^{-1}(x) = \frac{-5 - 3x}{5}$   
 85)  $g^{-1}(x) = \frac{-3x - 7}{2}$   
 89)  $f^{-1}(x) = \frac{15 + 4x}{3}$   
 93)  $g^{-1}(x) = -\frac{2}{3}x + \frac{4}{3}$   
 97)  $g^{-1}(x) = \frac{-12 + x}{3}$   
 101)  $f^{-1}(x) = -2x^5 + 3$   
 104)  $f^{-1}(n) = (n - 2)^3$   
  
 107)  $g^{-1}(x) = x^3 - 1$   
 110)  $f^{-1}(x) = -2x^3$   
 113)  $g^{-1}(x) = \sqrt[3]{\frac{-x - 1}{2}}$   
  
 2)  $3n + 6$   
 6)  $x^3 + 3x^2 - 2x + 4$   
 10)  $a^2 + 4a - 3$   
 14)  $-a^3 - 7a^2 - 10a$   
 18)  $3n^3 - 4n^2 + 12n - 16$   
 21)  $-1$   
  
 25)  $\frac{4n + 3}{-2n^2 - 2n}$   
 29)  $\frac{2x - 5}{x + 2}$   
 33)  $-20n - 21$   
 37)  $-14n - 19$   
 40)  $-5x^3 - 24x - 4$   
 44)  $3a^2 + 11$   
 48)  $4x - 11$   
 52)  $-27x^2 + 3$   
 55)  $16t - 9$   
 59)  $x^2 + 2$   
 62)  $-42$   
 66)  $-70$   
 70)  $0$   
  
 74)  $\frac{41}{44}$   
 78)  $2$   
 82)  $f^{-1}(n) = -n - 1$   
 86)  $g^{-1}(x) = -1 - \frac{4}{3}x$   
 90)  $g^{-1}(n) = -4n - 4$   
 94)  $g^{-1}(n) = -3n - 5$   
 98)  $f^{-1}(x) = \frac{-3x - 15}{10}$   
 102)  $f^{-1}(n) = 2n^3 - 3$   
 105)  $h^{-1}(x) = \sqrt[3]{\frac{x + 3}{2}}$   
 108)  $g^{-1}(x) = 2x^5$   
 111)  $g^{-1}(x) = (x - 2)^5$   
 114)  $g^{-1}(n) = -3 - 2n^3$   
  
 3)  $-x^3 - 7x - 3$   
 7)  $n^2 + 2n - 7$   
 11)  $-4x^3 + 12x$   
 15)  $4a^3 + 2a^2 + 4a + 2$   
 19)  $3a^3 - 2a^2 - 12a + 8$   
 22)  $\frac{x^2 + 5}{3x + 3}$   
 26)  $\frac{t^3 + t^2}{t + 4}$   
 30)  $\frac{3x + 2}{x^3 - 4}$   
 34)  $5n^3 + 4n - 5$   
 38)  $-8t^3 - 16t^2 - 12t - 20$   
 41)  $-4t^3 - 8t^2 + 2$   
 45)  $3x^3 + 15x^2 - 5$   
 49)  $2a^3 - 10a + 2$   
 53)  $x + 5$   
 56)  $2t - 2$   
 60)  $4x^2 - 19$   
 63)  $78$   
 67)  $56$   
 71)  $-\frac{13}{23}$   
 75)  $-10$   
 79)  $-5$   
 83)  $g^{-1}(x) = \frac{x - 3}{3}$   
 87)  $g^{-1}(n) = \frac{-2n - 2}{5}$   
 91)  $f^{-1}(x) = 3x - 1$   
 95)  $h^{-1}(x) = x + 2$   
 99)  $g^{-1}(x) = \frac{-15 - 3x}{5}$   
 103)  $g^{-1}(n) = (n + 1)^5 + 2$   
 106)  $f^{-1}(n) = (n + 1)^5 + 1$   
 109)  $g^{-1}(x) = \frac{4 + \sqrt[5]{16x}}{2}$   
 112)  $g^{-1}(n) = n^5$   
 115)  $f^{-1}(x) = \sqrt[3]{-\frac{x}{2}}$

116)  $g^{-1}(x) = \frac{-2 + \sqrt[3]{4x}}{2}$

119)  $g^{-1}(x) = -3 + (x - 2)^3$

122)  $g^{-1}(x) = \frac{1}{x-1} - 2$

125)  $f^{-1}(n) = \frac{4}{n} - 1$

128)  $h^{-1}(x) = -\frac{4}{x-1} + 1$

131)  $f^{-1}(n) = \frac{2}{n+3}$

134)  $f^{-1}(x) = -\frac{2}{x+1} + 3$

137)  $f^{-1}(x) = \frac{2}{x} - 3$

140)  $g^{-1}(x) = -\frac{3}{x+3} + 1$

143)  $f^{-1}(x) = \frac{9x-1}{x+7}$

147) No

151) No

155) No

159) Yes

163) No

117)  $g^{-1}(n) = 1 - 2n^3$

120)  $g^{-1}(x) = \sqrt[3]{\frac{-x+1}{2}}$

123)  $g^{-1}(x) = -\frac{4}{x-2} + 1$

126)  $g^{-1}(n) = \frac{2}{-n+2} + 2$

129)  $g^{-1}(n) = -\frac{3}{n+2} + 2$

132)  $f^{-1}(x) = \frac{4}{x-2} - 2$

135)  $f^{-1}(x) = \frac{1}{x-2} - 3$

138)  $g^{-1}(x) = \frac{1}{-x+1} + 2$

141)  $g^{-1}(x) = \frac{5x+5}{x-1}$

144)  $g^{-1}(x) = \frac{5x+4}{2x-1}$

148) No

152) Yes

156) No

160) Yes

164) Yes

149) No

153) No

157) Yes

161) Yes

165)

118)  $g^{-1}(n) = (n+1)^3$

121)  $f^{-1}(x) = -\frac{3}{x-2} + 2$

124)  $g^{-1}(x) = -\frac{2}{x}$

127)  $f^{-1}(x) = \frac{3}{x-1} - 1$

130)  $g^{-1}(x) = -\frac{2}{-x-2} + 2$

133)  $g^{-1}(x) = -\frac{3}{x+1} - 3$

136)  $f^{-1}(n) = -\frac{2}{-n-2}$

139)  $g^{-1}(n) = \frac{1}{n-2} - 1$

142)  $g^{-1}(x) = \frac{7}{x+2}$

145) Yes

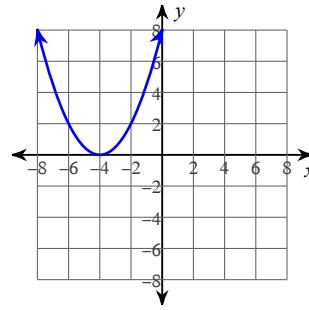
146) Yes

150) Yes

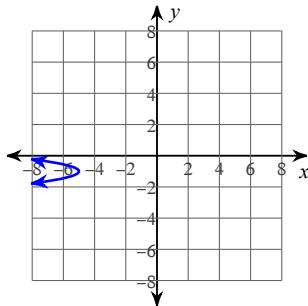
154) Yes

158) Yes

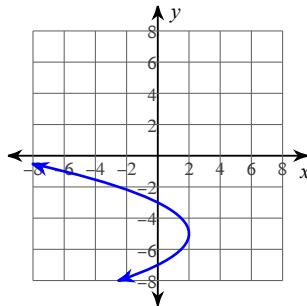
162) No



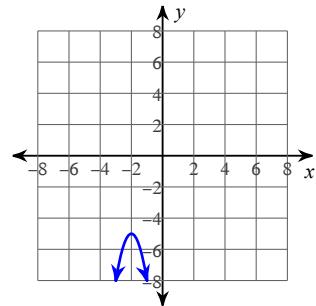
166)



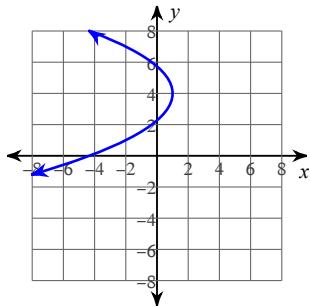
167)



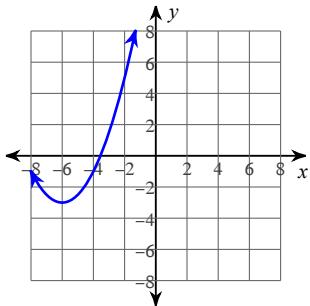
168)



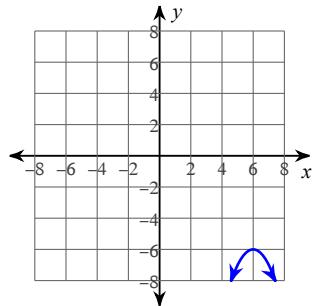
169)



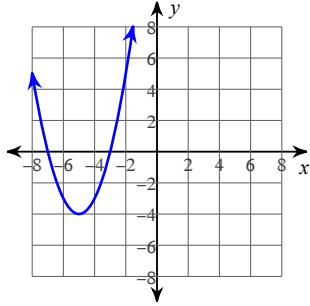
170)



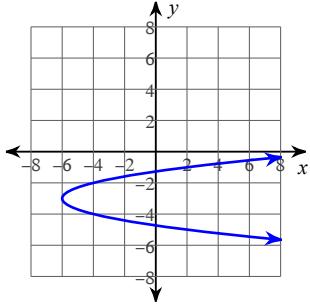
171)



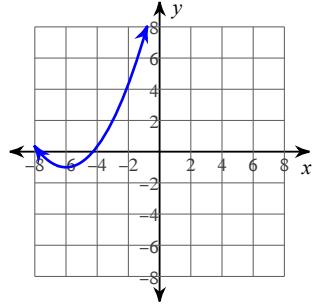
172)



173)



174)



175)  $y = -5(x - 8)^2 + 4$

176)  $y = -\frac{1}{3}x^2 - 8$

177)  $x = -2(y + 6)^2 + 9$

178)  $x = -\frac{1}{2}y^2 + 4$

179)  $x = -3(y - 10)^2 + 1$

180)  $y = -(x - 1)^2 + 9$

181)  $y = -8(x - 3)^2 + 3$

182)  $y = -8(x - 8)^2 + 4$

183)  $x = -2(y - 10)^2 - 5$

184)  $x = \frac{3}{4}(y + 9)^2 - 10$

185)  $x = -y^2 - 4$

186)  $y = -\frac{1}{4}(x - 10)^2 - 3$

187)  $x = -(y - 10)^2 + 1$

188)  $x = -(y - 6)^2 + 9$

189)  $y = (x - 3)^2 + 4$

190)  $x = \frac{1}{4}(y - 3)^2 + 1$

191)  $x = 5(y - 10)^2 - 6$

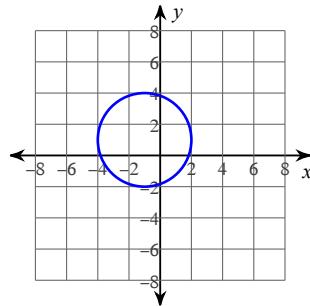
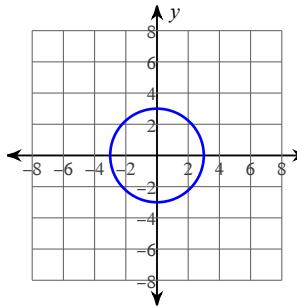
192)  $y = \frac{1}{4}(x + 2)^2 - 5$

193)  $x = -4(y - 3)^2 - 10$

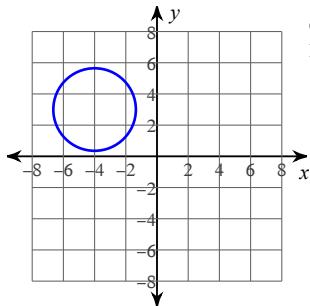
194)  $x = 2(y + 7)^2 - 5$

195)

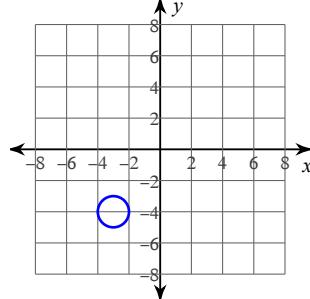
196)



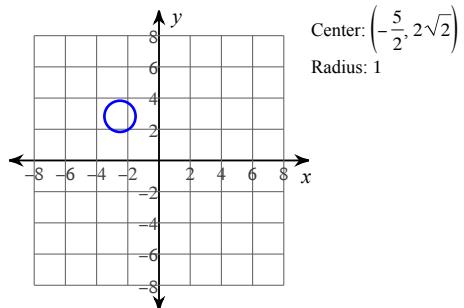
197)

Center:  $(-4, 3)$   
Radius:  $\sqrt{7}$ 

198)

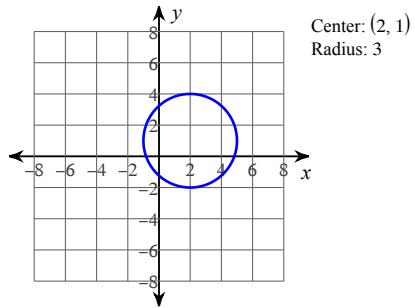
Center:  $(-3, -4)$   
Radius: 1

199)



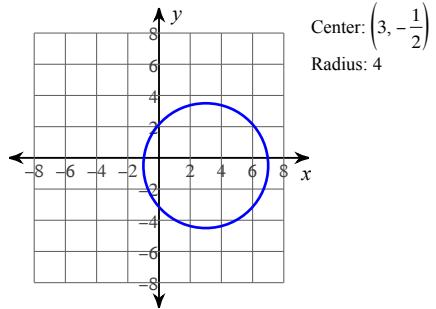
Center:  $\left(-\frac{5}{2}, 2\sqrt{2}\right)$   
Radius: 1

201)



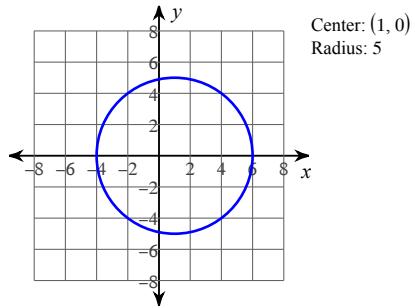
Center:  $(2, 1)$   
Radius: 3

203)



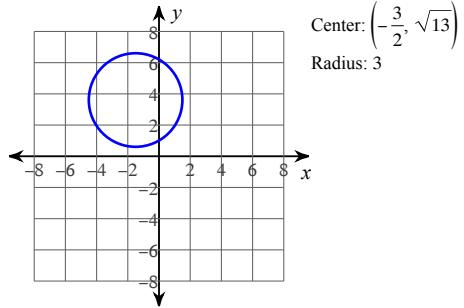
Center:  $\left(3, -\frac{1}{2}\right)$   
Radius: 4

205)



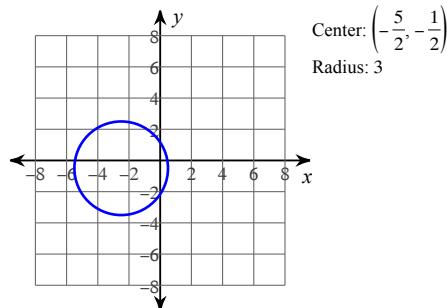
Center:  $(1, 0)$   
Radius: 5

207)



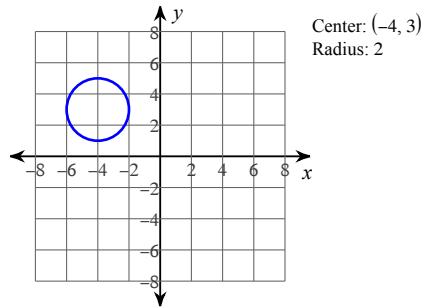
Center:  $\left(\frac{3}{2}, \sqrt{13}\right)$   
Radius: 3

200)



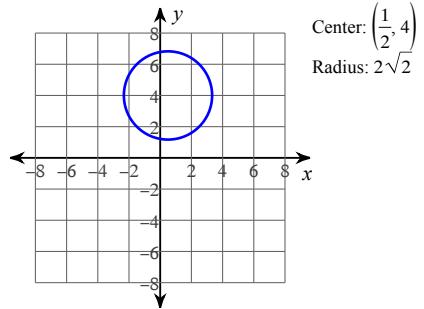
Center:  $\left(-\frac{5}{2}, -\frac{1}{2}\right)$   
Radius: 3

202)



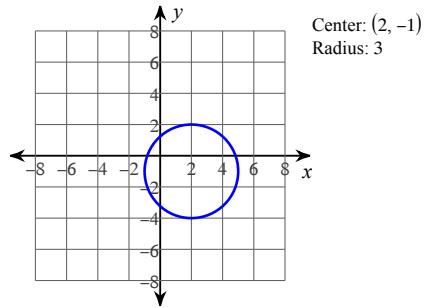
Center:  $(-4, 3)$   
Radius: 2

204)



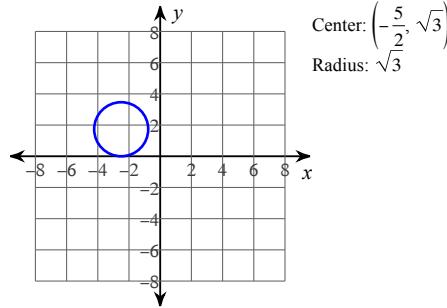
Center:  $\left(\frac{1}{2}, 4\right)$   
Radius:  $2\sqrt{2}$

206)



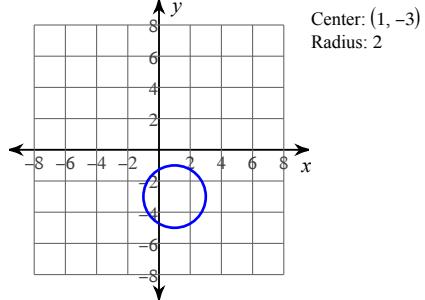
Center:  $(2, -1)$   
Radius: 3

208)

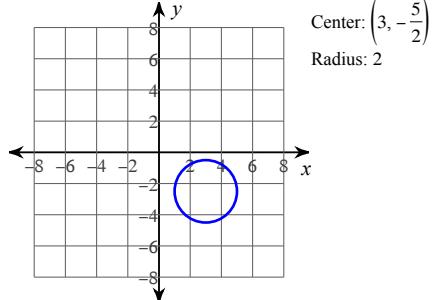


Center:  $\left(-\frac{5}{2}, \sqrt{3}\right)$   
Radius:  $\sqrt{3}$

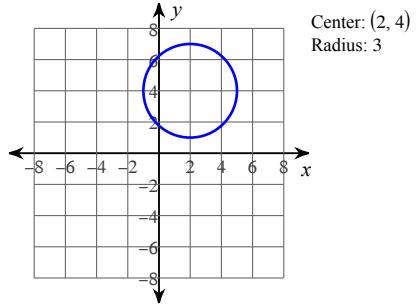
209)

Center:  $(1, -3)$   
Radius: 2

211)

Center:  $(3, -\frac{5}{2})$   
Radius: 2

213)

Center:  $(2, 4)$   
Radius: 3

215)  $(x - 16)^2 + (y + 10)^2 = 4$

216)  $(x - 11)^2 + (y + 4)^2 = 36$

218)  $(x - 4\sqrt{11})^2 + (y + 13)^2 = 4$

220)  $(x + 2)^2 + (y - 7)^2 = 41$

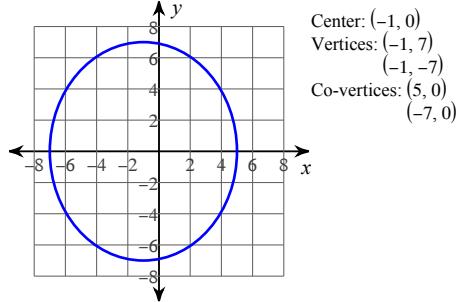
223)  $(x + 5)^2 + (y + 4)^2 = 1$

226)  $(x - 10)^2 + (y - 4)^2 = 81$

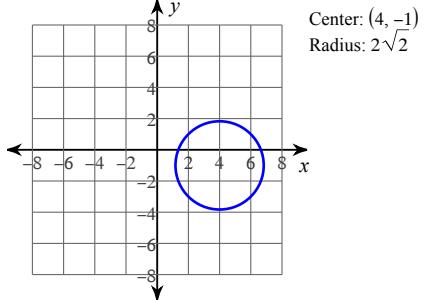
229)  $(x + 9)^2 + (y - 12)^2 = 16$

232)  $(x + 10)^2 + (y - 14)^2 = 17$

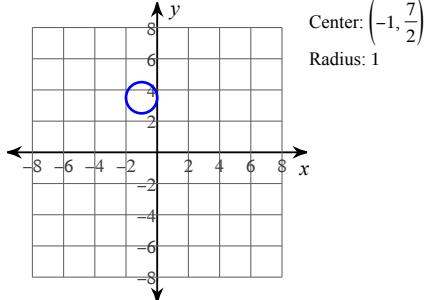
235)

Center:  $(-1, 0)$   
Vertices:  $(-1, 7)$   
 $(-1, -7)$   
Co-vertices:  $(5, 0)$   
 $(-7, 0)$ 

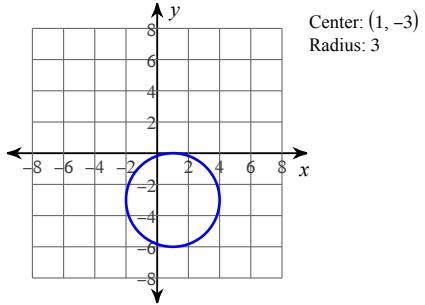
210)

Center:  $(4, -1)$   
Radius:  $2\sqrt{2}$ 

212)

Center:  $(-1, \frac{7}{2})$   
Radius: 1

214)

Center:  $(1, -3)$   
Radius: 3

217)  $(x + 15)^2 + \left(y - \frac{1}{2}\right)^2 = 16$

219)  $\left(x + \frac{13}{2}\right)^2 + \left(y - \frac{1}{2}\right)^2 = 100$

221)  $(x + 5)^2 + (y + 11)^2 = 5$

222)  $(x - 13)^2 + (y + 6)^2 = 36$

224)  $(x + 14)^2 + (y + 14)^2 = 4$

225)  $(x - 4)^2 + (y - 13)^2 = 19$

227)  $(x + 2)^2 + (y + 9)^2 = 100$

228)  $(x - 15)^2 + (y - 6)^2 = 16$

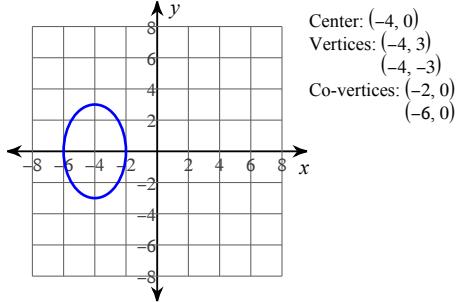
230)  $(x - 13)^2 + (y + 10)^2 = 31$

231)  $(x - 4)^2 + (y - 13)^2 = 9$

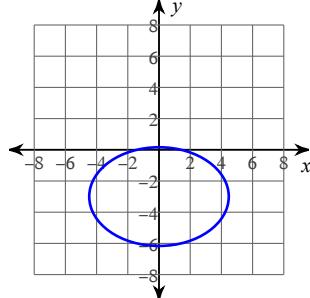
233)  $x^2 + (y - 15)^2 = 1$

234)  $x^2 + (y - 15)^2 = 9$

236)

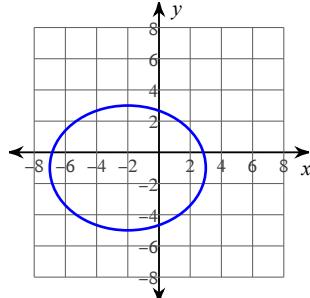
Center:  $(-4, 0)$   
Vertices:  $(-4, 3)$   
 $(-4, -3)$   
Co-vertices:  $(-2, 0)$   
 $(-6, 0)$

237)



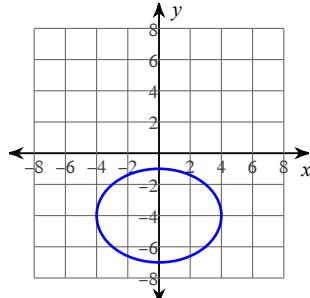
Center:  $(0, -3)$   
 Vertices:  $(2\sqrt{5}, -3)$   
 $(-2\sqrt{5}, -3)$   
 Co-vertices:  $(0, -3 + \sqrt{10})$   
 $(0, -3 - \sqrt{10})$

239)



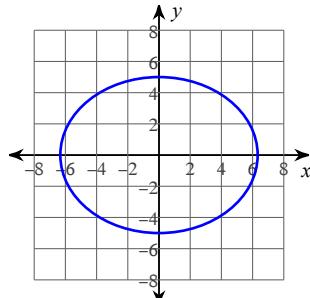
Center:  $(-2, -1)$   
 Vertices:  $(3, -1)$   
 $(-7, -1)$   
 Co-vertices:  $(-2, 3)$   
 $(-2, -5)$

241)



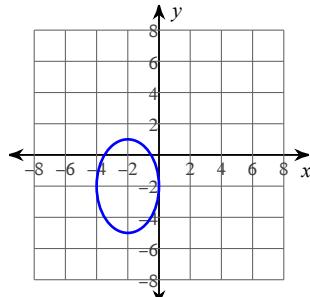
Center:  $(0, -4)$   
 Vertices:  $(4, -4)$   
 $(-4, -4)$   
 Co-vertices:  $(0, -1)$   
 $(0, -7)$

243)



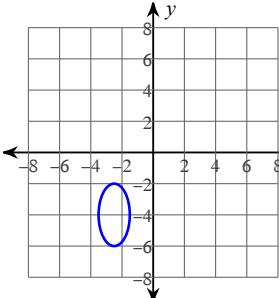
Center:  $(0, 0)$   
 Vertices:  $(2\sqrt{10}, 0)$   
 $(-2\sqrt{10}, 0)$   
 Co-vertices:  $(0, 5)$   
 $(0, -5)$

245)



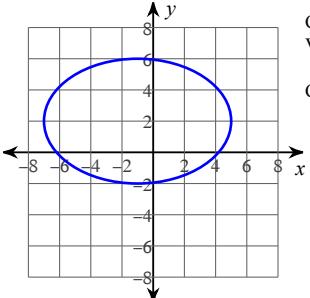
Center:  $(-2, -2)$   
 Vertices:  $(-2, 1)$   
 $(-2, -5)$   
 Co-vertices:  $(0, -2)$   
 $(-4, -2)$

238)



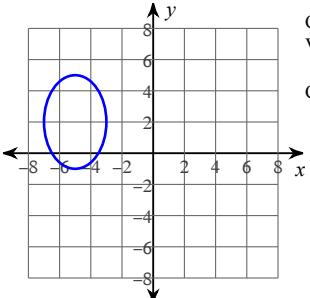
Center:  $(-\frac{5}{2}, -4)$   
 Vertices:  $(-\frac{5}{2}, -2)$   
 $(-\frac{5}{2}, -6)$   
 Co-vertices:  $(-\frac{3}{2}, -4)$   
 $(-\frac{7}{2}, -4)$

240)



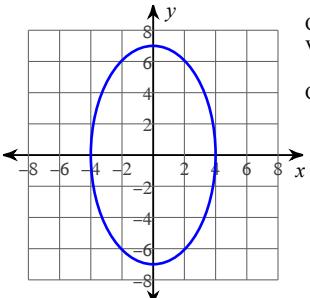
Center:  $(-1, 2)$   
 Vertices:  $(5, 2)$   
 $(-7, 2)$   
 Co-vertices:  $(-1, 6)$   
 $(-1, -2)$

242)



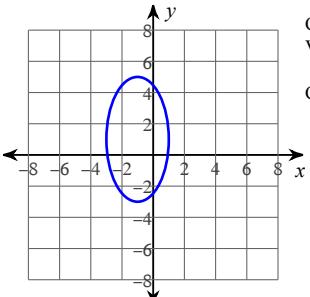
Center:  $(-5, 2)$   
 Vertices:  $(-5, 5)$   
 $(-5, -1)$   
 Co-vertices:  $(-3, 2)$   
 $(-7, 2)$

244)



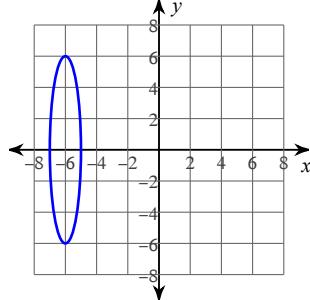
Center:  $(0, 0)$   
 Vertices:  $(0, 7)$   
 $(0, -7)$   
 Co-vertices:  $(4, 0)$   
 $(-4, 0)$

246)



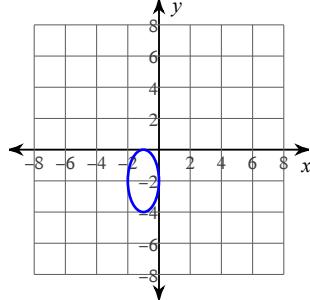
Center:  $(-1, 1)$   
 Vertices:  $(-1, 5)$   
 $(-1, -3)$   
 Co-vertices:  $(1, 1)$   
 $(-3, 1)$

247)



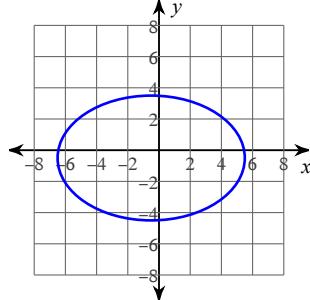
Center:  $(-6, 0)$   
 Vertices:  $(-6, 6)$   
 $(-6, -6)$   
 Co-vertices:  $(-5, 0)$   
 $(-7, 0)$

249)



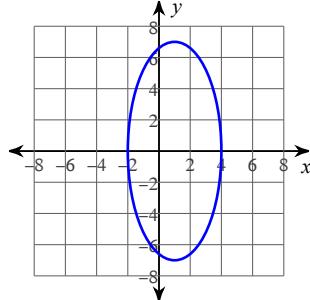
Center:  $(-1, -2)$   
 Vertices:  $(-1, 0)$   
 $(-1, -4)$   
 Co-vertices:  $(0, -2)$   
 $(-2, -2)$

251)



Center:  $\left(-\frac{1}{2}, -\frac{1}{2}\right)$   
 Vertices:  $\left(\frac{11}{2}, -\frac{1}{2}\right)$   
 $\left(-\frac{13}{2}, -\frac{1}{2}\right)$   
 Co-vertices:  $\left(-\frac{1}{2}, \frac{7}{2}\right)$   
 $\left(-\frac{1}{2}, -\frac{9}{2}\right)$

253)



Center:  $(1, 0)$   
 Vertices:  $(1, 7)$   
 $(1, -7)$   
 Co-vertices:  $(4, 0)$   
 $(-2, 0)$

$$255) \frac{(x-6)^2}{25} + \frac{(y+4)^2}{4} = 1$$

$$258) \frac{(x-5)^2}{64} + \frac{(y+2)^2}{121} = 1$$

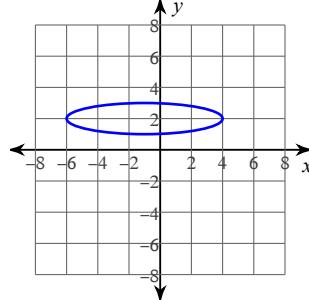
$$261) \frac{(x+1)^2}{121} + \frac{(y+3)^2}{100} = 1$$

$$264) \frac{(x+7)^2}{4} + \frac{(y+9)^2}{16} = 1$$

$$267) \frac{x^2}{16} + \frac{(y-4)^2}{64} = 1$$

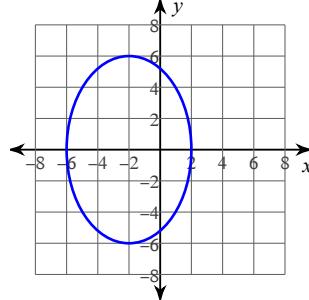
$$270) \frac{\left(x+\frac{5}{2}\right)^2}{144} + \frac{(y+7)^2}{64} = 1$$

248)



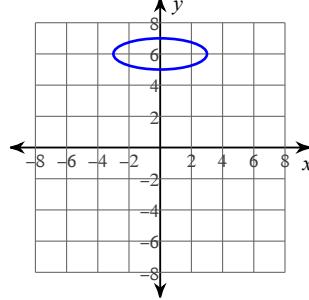
Center:  $(-1, 2)$   
 Vertices:  $(4, 2)$   
 $(-6, 2)$   
 Co-vertices:  $(-1, 3)$   
 $(-1, 1)$

250)



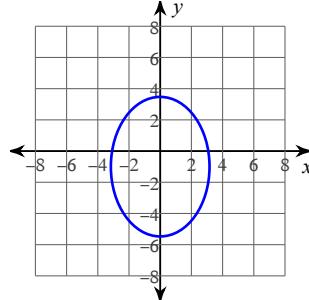
Center:  $(-2, 0)$   
 Vertices:  $(-2, 6)$   
 $(-2, -6)$   
 Co-vertices:  $(2, 0)$   
 $(-6, 0)$

252)



Center:  $(0, 6)$   
 Vertices:  $(3, 6)$   
 $(-3, 6)$   
 Co-vertices:  $(0, 7)$   
 $(0, 5)$

254)



Center:  $(0, -1)$   
 Vertices:  $(0, -1 + 2\sqrt{5})$   
 $(0, -1 - 2\sqrt{5})$   
 Co-vertices:  $(\sqrt{10}, -1)$   
 $(-\sqrt{10}, -1)$

$$256) \frac{(x+2)^2}{81} + \frac{(y+5)^2}{16} = 1$$

$$259) \frac{(x-4)^2}{121} + \frac{(y+8)^2}{64} = 1$$

$$262) \frac{(x-8)^2}{25} + \frac{(y-2)^2}{36} = 1$$

$$265) \frac{(x+1)^2}{25} + \frac{(y-9)^2}{81} = 1$$

$$268) \frac{(x+3)^2}{144} + \frac{(y-3)^2}{4} = 1$$

$$271) \frac{(x-7)^2}{49} + \frac{(y-2)^2}{225} = 1$$

$$257) \frac{(x+9)^2}{16} + \frac{(y+8)^2}{121} = 1$$

$$260) \frac{(x+2)^2}{100} + \frac{(y-3)^2}{49} = 1$$

$$263) \frac{(x+5)^2}{225} + \frac{(y-5)^2}{81} = 1$$

$$266) \frac{(x+2)^2}{100} + \frac{(y-5)^2}{121} = 1$$

$$269) \frac{(x-4)^2}{125} + \frac{(y-9)^2}{55} = 1$$

$$272) \frac{(x+2)^2}{169} + \frac{(y-5)^2}{64} = 1$$

273)  $\frac{(x-1)^2}{81} + \frac{(y+5)^2}{9} = 1$

276)  $\frac{(x-7)^2}{9} + \frac{(y+2)^2}{36} = 1$

279)  $\frac{(x+2)^2}{36} + \frac{(y+10)^2}{81} = 1$

282)  $\frac{x^2}{25} + \frac{(y-4)^2}{16} = 1$

285)  $\frac{(x-3)^2}{144} + \frac{(y-2)^2}{36} = 1$

288)  $\frac{(x+7)^2}{25} + \frac{(y-4)^2}{100} = 1$

291)  $\frac{(x+8)^2}{90} + \frac{(y-2)^2}{5} = 1$

294)  $\frac{(x-5)^2}{49} + \frac{y^2}{9} = 1$       295)

274)  $\frac{(x-6)^2}{115} + \frac{(y+2)^2}{75} = 1$

277)  $\frac{(x+10)^2}{100} + \frac{(y-3)^2}{64} = 1$

280)  $\frac{\left(x+\frac{15}{2}\right)^2}{60} + \frac{\left(y+\frac{7}{2}\right)^2}{75} = 1$

283)  $\frac{(x+6)^2}{144} + \frac{(y+5)^2}{36} = 1$

286)  $\frac{(x-4)^2}{100} + \frac{(y-8)^2}{64} = 1$

289)  $\frac{(x-4)^2}{20} + \frac{(y-1)^2}{115} = 1$

292)  $\frac{(x+4)^2}{4} + \frac{(y+7)^2}{36} = 1$

275)  $\frac{(x+3)^2}{49} + \frac{(y-4)^2}{196} = 1$

278)  $\frac{(x-5)^2}{81} + \frac{(y+3)^2}{36} = 1$

281)  $\frac{(x-6)^2}{16} + \frac{(y+5)^2}{144} = 1$

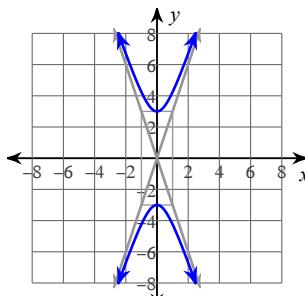
284)  $\frac{(x+8)^2}{144} + \frac{(y+4)^2}{36} = 1$

287)  $\frac{x^2}{16} + \frac{(y-5)^2}{100} = 1$

290)  $\frac{x^2}{144} + \frac{(y-5)^2}{36} = 1$

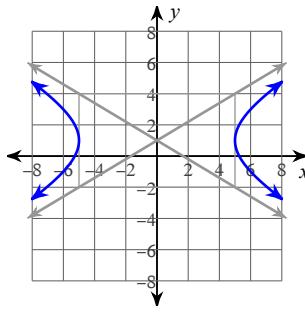
293)  $\frac{(x-6)^2}{64} + \frac{(y-4)^2}{36} = 1$

296)

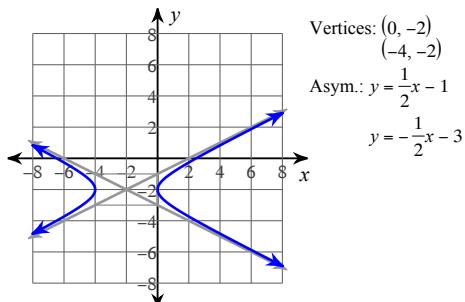


Vertices:  $(0, 3)$   
 $(0, -3)$   
Asym.:  $y = 3x$   
 $y = -3x$

298)

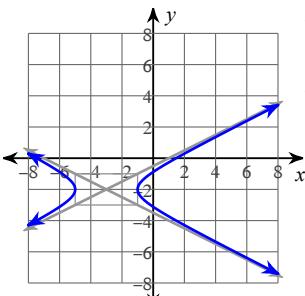


Vertices:  $(5, 1)$   
 $(-5, 1)$   
Asym.:  $y = \frac{3}{5}x + 1$   
 $y = -\frac{3}{5}x + 1$



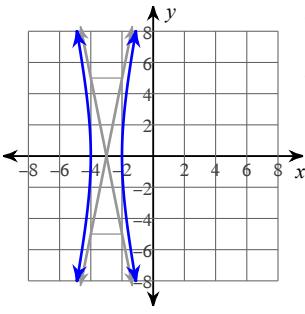
Vertices:  $(0, -2)$   
 $(-4, -2)$   
Asym.:  $y = \frac{1}{2}x - 1$   
 $y = -\frac{1}{2}x - 3$

297)



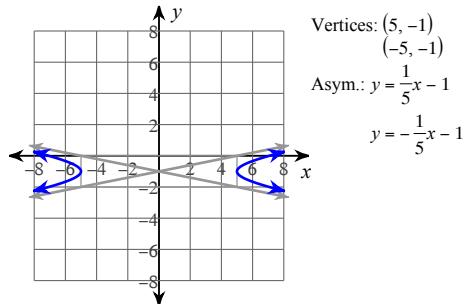
Vertices:  $(-1, -2)$   
 $(-5, -2)$   
Asym.:  $y = \frac{1}{2}x - \frac{1}{2}$   
 $y = -\frac{1}{2}x - \frac{7}{2}$

299)

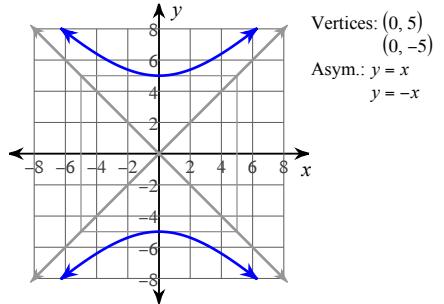


Vertices:  $(-2, 0)$   
 $(-4, 0)$   
Asym.:  $y = 5x + 15$   
 $y = -5x - 15$

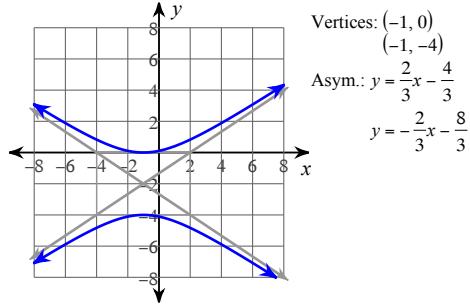
300)



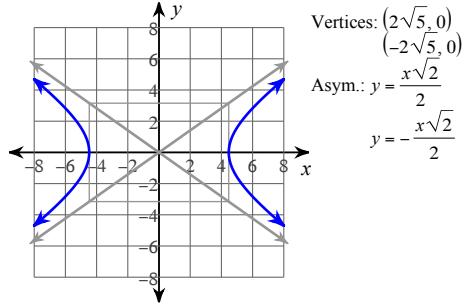
302)



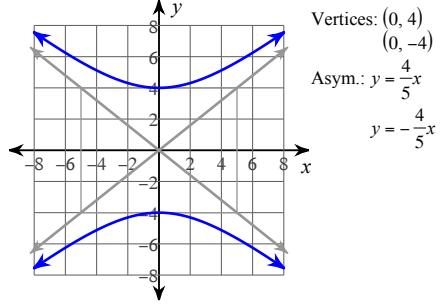
304)



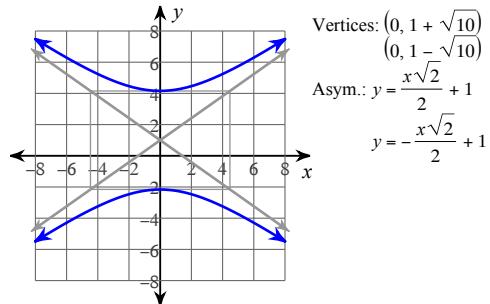
306)



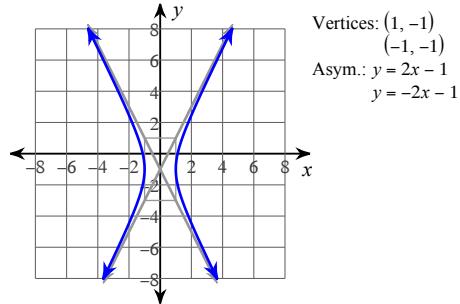
308)



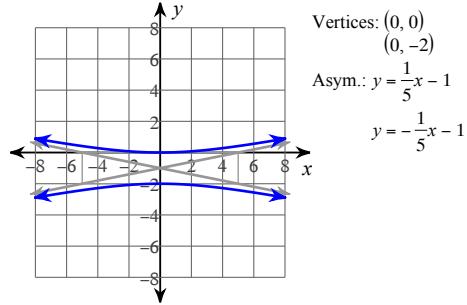
301)



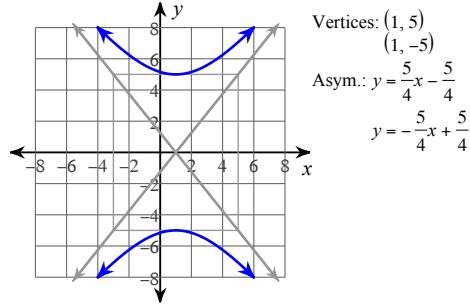
303)



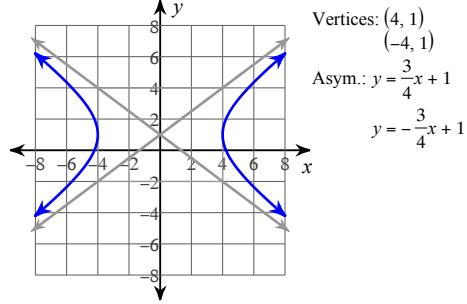
305)



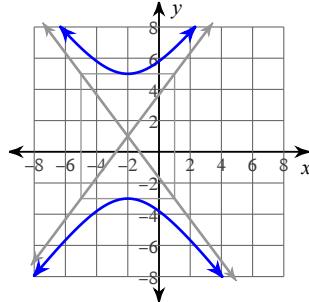
307)



309)

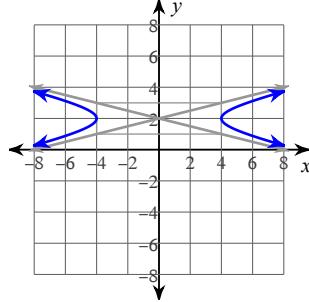


310)



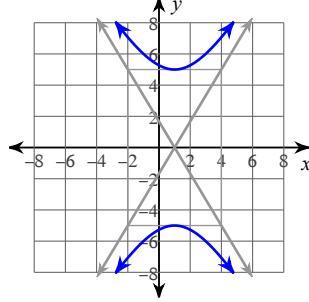
Vertices:  $(-2, 5)$   
 $(-2, -3)$   
 Asym.:  $y = \frac{4}{3}x + \frac{11}{3}$   
 $y = -\frac{4}{3}x - \frac{5}{3}$

312)



Vertices:  $(4, 2)$   
 $(-4, 2)$   
 Asym.:  $y = \frac{1}{4}x + 2$   
 $y = -\frac{1}{4}x + 2$

314)



Vertices:  $(1, 5)$   
 $(1, -5)$   
 Asym.:  $y = \frac{5}{3}x - \frac{5}{3}$   
 $y = -\frac{5}{3}x + \frac{5}{3}$

$$316) \frac{(y+8)^2}{36} - \frac{(x+6)^2}{25} = 1$$

$$319) \frac{(y-8)^2}{196} - \frac{(x-7)^2}{64} = 1$$

$$322) \frac{(y-7)^2}{169} - \frac{(x-2)^2}{16} = 1$$

$$325) \frac{(y-6)^2}{20} - \frac{(x-6)^2}{10} = 1$$

$$328) \frac{(x+1)^2}{36} - \frac{(y-2)^2}{49} = 1$$

$$331) \frac{(y+8)^2}{121} - \frac{(x+6)^2}{100} = 1$$

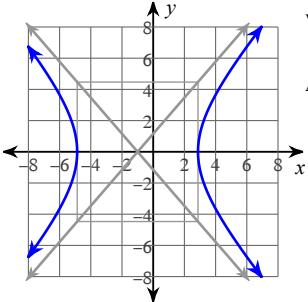
$$334) \frac{(y+1)^2}{64} - \frac{(x+9)^2}{169} = 1$$

$$337) \frac{(y+7)^2}{36} - \frac{(x+5)^2}{225} = 1$$

$$340) \frac{(x-6)^2}{144} - \frac{(y+2)^2}{36} = 1$$

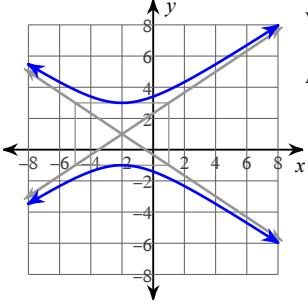
$$343) \frac{(y+7)^2}{36} - \frac{(x-3)^2}{25} = 1$$

311)



Vertices:  $(-1 + \sqrt{15}, 0)$   
 $(-1 - \sqrt{15}, 0)$   
 Asym.:  $y = \frac{2x\sqrt{3}}{3} + \frac{2\sqrt{3}}{3}$   
 $y = -\frac{2x\sqrt{3}}{3} - \frac{2\sqrt{3}}{3}$

313)



Vertices:  $(-2, 3)$   
 $(-2, -1)$   
 Asym.:  $y = \frac{2}{3}x + \frac{7}{3}$   
 $y = -\frac{2}{3}x - \frac{1}{3}$

$$315) \frac{(y+2)^2}{16} - \frac{(x+7)^2}{4} = 1$$

$$317) \frac{(y+7)^2}{80} - \frac{(x+8)^2}{105} = 1$$

$$320) \frac{(x+10)^2}{49} - \frac{(y-6)^2}{121} = 1$$

$$323) \frac{(x-1)^2}{81} - \frac{(y-9)^2}{9} = 1$$

$$326) \frac{x^2}{49} - \frac{(y-6)^2}{36} = 1$$

$$329) \frac{(x-10)^2}{64} - \frac{(y-5)^2}{64} = 1$$

$$332) \frac{(x+7)^2}{144} - \frac{(y+6)^2}{16} = 1$$

$$335) \frac{(x+6)^2}{36} - \frac{(y-3)^2}{144} = 1$$

$$338) \frac{(x-5)^2}{25} - \frac{(y+2)^2}{36} = 1$$

$$341) \frac{(x+8)^2}{36} - \frac{(y+2)^2}{81} = 1$$

$$344) \frac{(y-2)^2}{25} - \frac{(x+1)^2}{16} = 1$$

$$318) \frac{(y-6)^2}{105} - \frac{(x+1)^2}{150} = 1$$

$$321) \frac{(x-1)^2}{110} - \frac{(y+2)^2}{200} = 1$$

$$324) \frac{(y+2)^2}{36} - \frac{(x-1)^2}{36} = 1$$

$$327) \frac{(x-5)^2}{49} - \frac{(y-4)^2}{100} = 1$$

$$330) \frac{(y-4)^2}{144} - \frac{(x-9)^2}{144} = 1$$

$$333) \frac{(y-2)^2}{4} - \frac{(x+6)^2}{196} = 1$$

$$336) \frac{(y-10)^2}{81} - \frac{(x+7)^2}{144} = 1$$

$$339) \frac{(y-2)^2}{225} - \frac{(x-4)^2}{25} = 1$$

$$342) \frac{x^2}{36} - \frac{(y-10)^2}{36} = 1$$

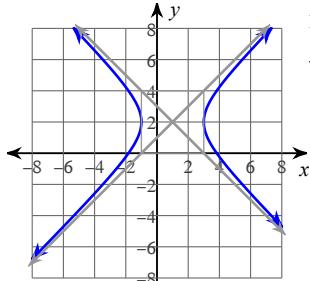
$$345) \frac{(x-10)^2}{16} - \frac{(y+4)^2}{16} = 1$$

346)  $\frac{(x+2)^2}{36} - \frac{y^2}{9} = 1$

349)  $\frac{(x+7)^2}{36} - \frac{(y+3)^2}{144} = 1$

352)  $\frac{(y+8)^2}{49} - \frac{(x+2)^2}{9} = 1$

355)

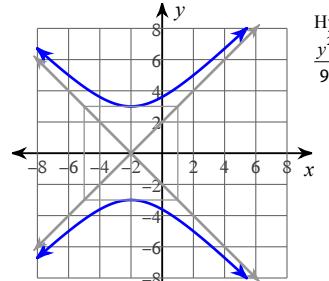


347)  $\frac{(y+1)^2}{36} - \frac{(x-4)^2}{144} = 1$

350)  $\frac{(x+6)^2}{16} - \frac{(y+3)^2}{144} = 1$

353)  $\frac{(x+7)^2}{100} - \frac{(y-5)^2}{100} = 1$

356)

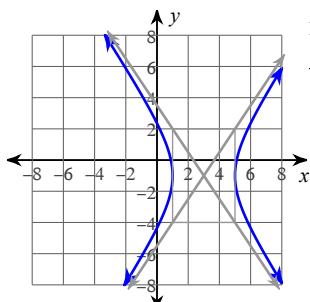


348)  $\frac{y^2}{36} - \frac{(x-1)^2}{144} = 1$

351)  $\frac{(y-3)^2}{144} - \frac{(x+3)^2}{36} = 1$

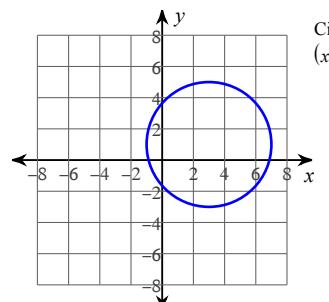
354)  $\frac{(x+1)^2}{100} - \frac{(y-5)^2}{25} = 1$

357)



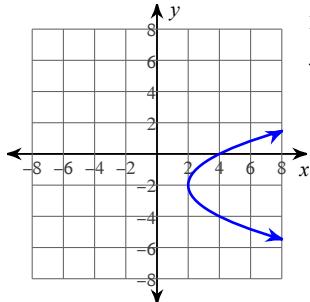
Hyperbola  
 $\frac{(x-3)^2}{4} - \frac{(y+1)^2}{9} = 1$

358)



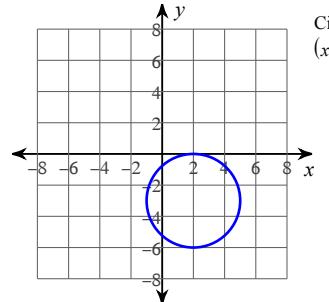
Circle  
 $(x-3)^2 + (y-1)^2 = 16$

359)



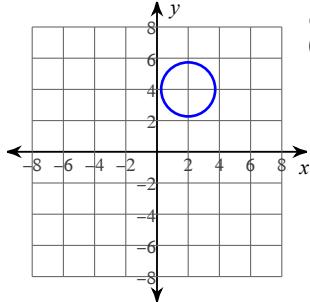
Parabola  
 $x = \frac{1}{2}(y+2)^2 + 2$

360)



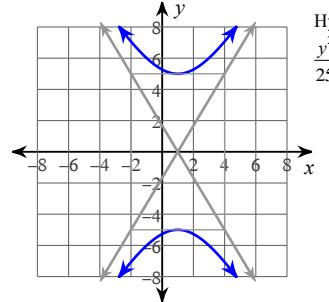
Circle  
 $(x-2)^2 + (y+3)^2 = 9$

361)



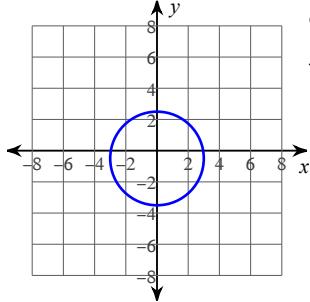
Circle  
 $(x-2)^2 + (y-4)^2 = 3$

362)



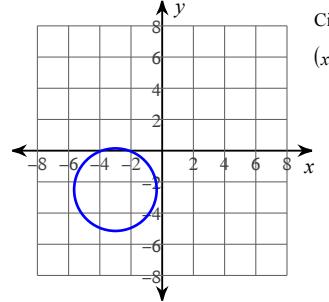
Hyperbola  
 $\frac{y^2}{25} - \frac{(x-1)^2}{9} = 1$

363)



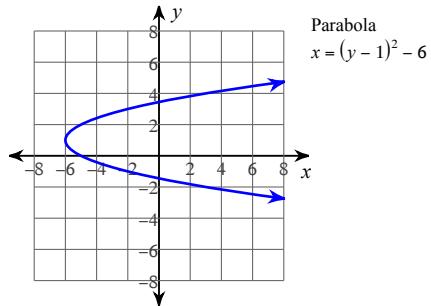
Circle  
 $x^2 + \left(y + \frac{1}{2}\right)^2 = 9$

364)



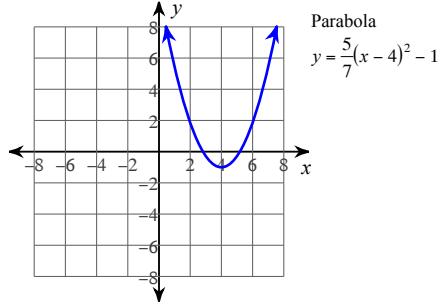
Circle  
 $(x+3)^2 + \left(y + \frac{5}{2}\right)^2 = 7$

365)



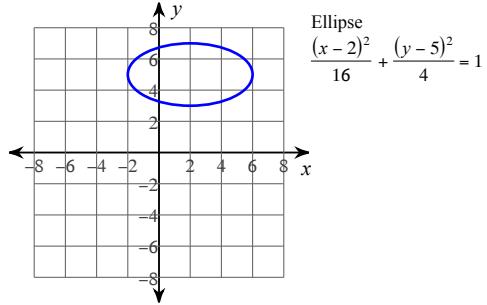
$$\text{Parabola } x = (y - 1)^2 - 6$$

367)



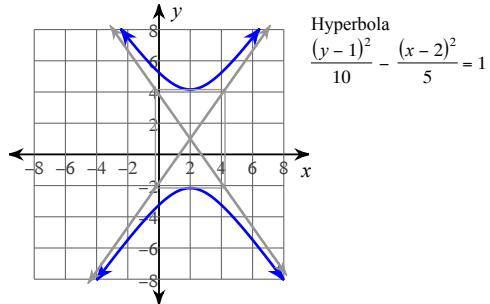
$$\text{Parabola } y = \frac{5}{7}(x - 4)^2 - 1$$

369)



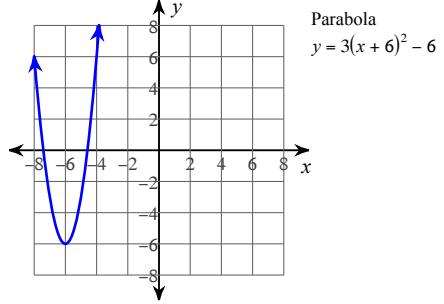
$$\text{Ellipse } \frac{(x - 2)^2}{16} + \frac{(y - 5)^2}{4} = 1$$

371)



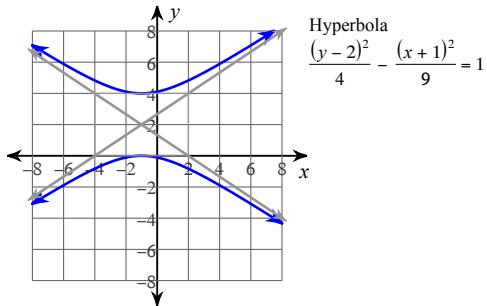
$$\text{Hyperbola } \frac{(y - 1)^2}{10} - \frac{(x - 2)^2}{5} = 1$$

373)



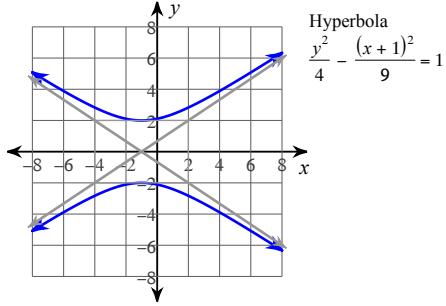
$$\text{Parabola } y = 3(x + 6)^2 - 6$$

366)



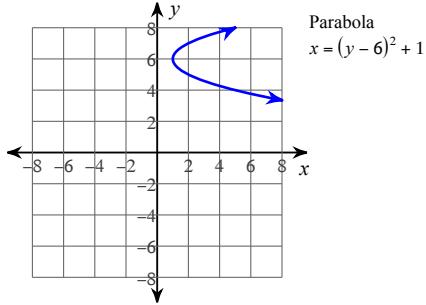
$$\text{Hyperbola } \frac{(y - 2)^2}{4} - \frac{(x + 1)^2}{9} = 1$$

368)



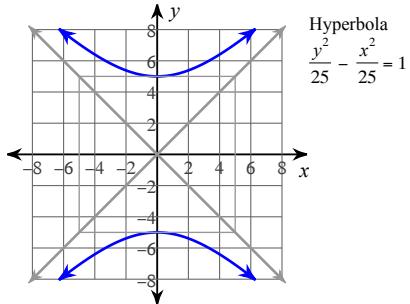
$$\text{Hyperbola } \frac{y^2}{4} - \frac{(x + 1)^2}{9} = 1$$

370)



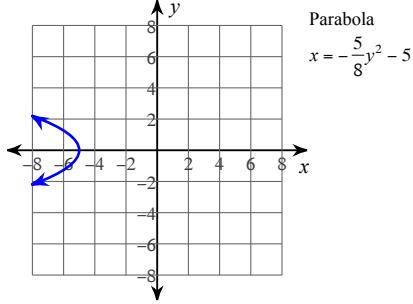
$$\text{Parabola } x = (y - 6)^2 + 1$$

372)



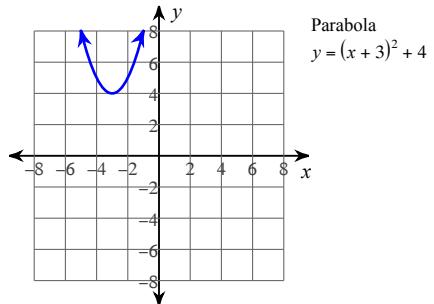
$$\text{Hyperbola } \frac{y^2}{25} - \frac{x^2}{25} = 1$$

374)



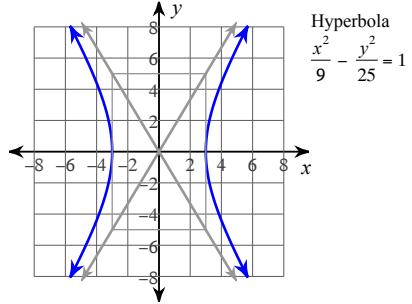
$$\text{Parabola } x = -\frac{5}{8}y^2 - 5$$

375)



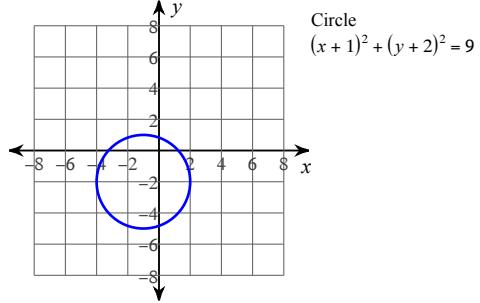
Parabola  
 $y = (x + 3)^2 + 4$

377)



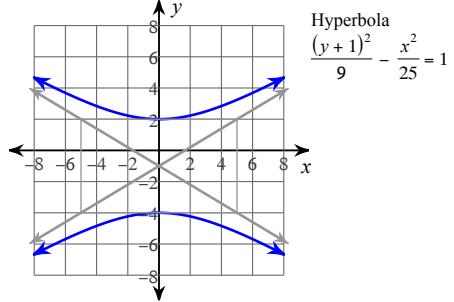
Hyperbola  
 $\frac{x^2}{9} - \frac{y^2}{25} = 1$

379)



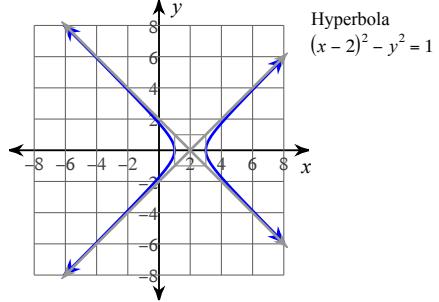
Circle  
 $(x + 1)^2 + (y + 2)^2 = 9$

381)



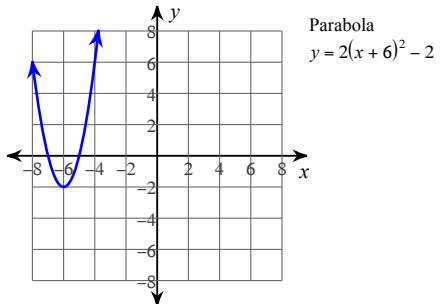
Hyperbola  
 $\frac{(y + 1)^2}{9} - \frac{x^2}{25} = 1$

383)



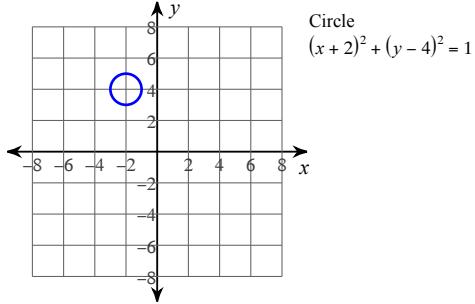
Hyperbola  
 $(x - 2)^2 - y^2 = 1$

376)



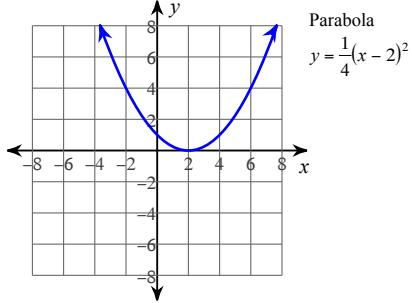
Parabola  
 $y = 2(x + 6)^2 - 2$

378)



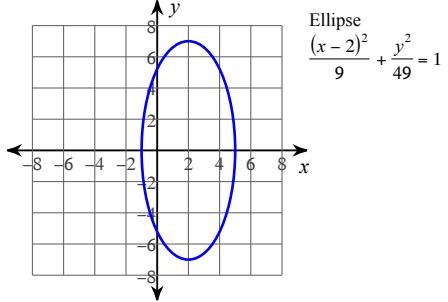
Circle  
 $(x + 2)^2 + (y - 4)^2 = 1$

380)



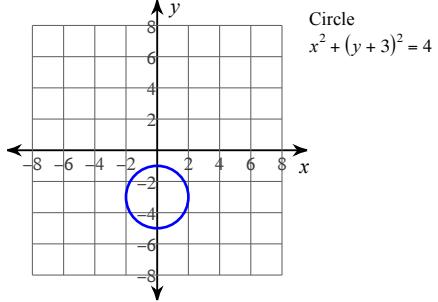
Parabola  
 $y = \frac{1}{4}(x - 2)^2$

382)



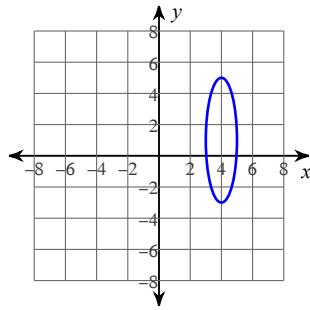
Ellipse  
 $\frac{(x - 2)^2}{9} + \frac{y^2}{49} = 1$

384)



Circle  
 $x^2 + (y + 3)^2 = 4$

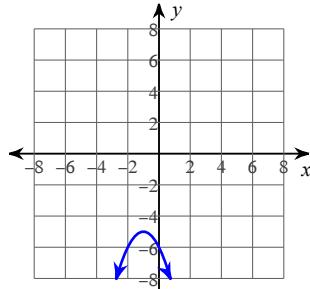
385)



Ellipse  

$$(x - 4)^2 + \frac{(y - 1)^2}{16} = 1$$

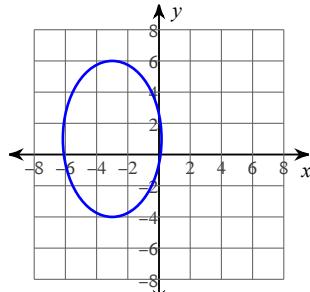
387)



Parabola  

$$y = -(x + 1)^2 - 5$$

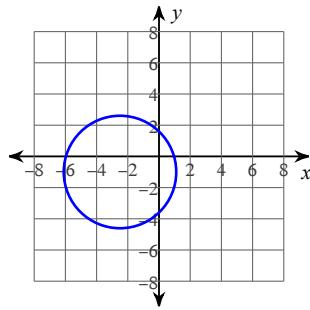
389)



Ellipse  

$$\frac{(x + 3)^2}{10} + \frac{(y - 1)^2}{25} = 1$$

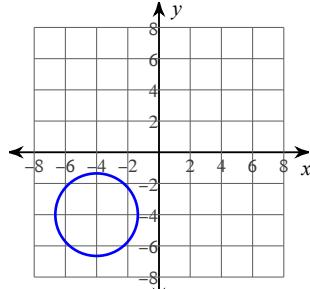
391)



Circle  

$$\left(x + \frac{5}{2}\right)^2 + (y + 1)^2 = 13$$

393)



Circle  

$$(x + 4)^2 + (y + 4)^2 = 7$$

395)  $(0, -4)$

399)  $(10, 8), (10, 4)$

402)  $(0, 4)$

405)  $(-1, 7), (-2, 9), (-2, 5)$

407)  $(9, -2), (9, -4), (-1, 0), (-1, -6)$

409) No solution.

412)  $(-2, -3), (5, -8), (-9, -8)$

415)  $(3, 7), (3, -1)$

396)  $(-2, 4)$

400)  $(1, -3)$

403)  $(-3, 1), (-7, 1)$

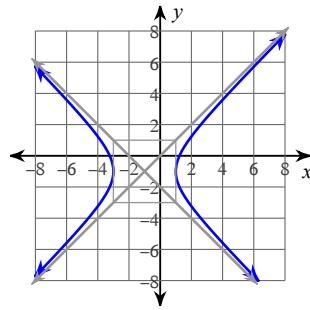
406)  $(-4, 2), (-6, 2), (-1, -2), (-9, -2)$

410)  $(7, -2), (10, -8), (4, -8)$

413)  $(4, 1)$

416)  $(7, -8), (9, 3), (5, 3)$

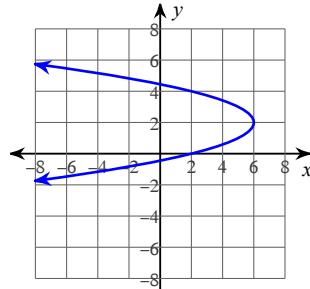
386)



Hyperbola  

$$\frac{(x + 1)^2}{4} - \frac{(y + 1)^2}{4} = 1$$

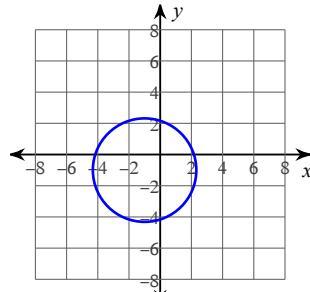
388)



Parabola  

$$x = -(y - 2)^2 + 6$$

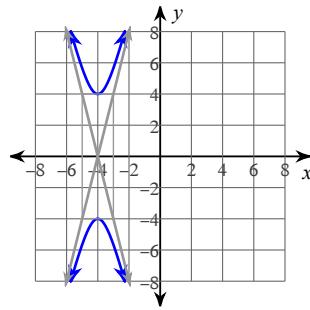
390)



Circle  

$$(x + 1)^2 + (y + 1)^2 = 11$$

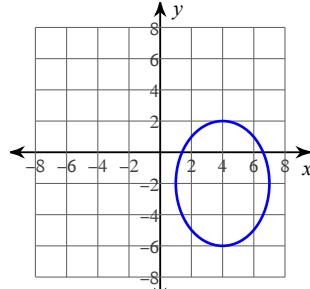
392)



Hyperbola  

$$\frac{y^2}{16} - (x + 4)^2 = 1$$

394)



Ellipse  

$$\frac{(x - 4)^2}{9} + \frac{(y + 2)^2}{16} = 1$$

397)  $(0, -1), (0, 1)$

401)  $(0, -6), (0, -10), (-10, -6), (-10, -10)$

404)  $(0, 6), (0, 2), (-2, 6), (-2, 2)$

408)  $(-3, 5), (-5, 5), (2, -1), (-10, -1)$

411)  $(-4, -9), (2, 6), (-10, 6)$

414)  $(-1, -6), (3, -3), (3, -9)$

417)  $(9, 2), (7, 2)$

398)  $(3, 5)$

- 418)  $(5, -4), (5, -8), (0, -5), (0, -7)$   
 420)  $(-6, -3), (-6, -7), (-2, -4), (-2, -6)$   
 423)  $(4, -5), (-4, -5), (4, 4), (-4, 4)$   
 425)  $(4, 5), (-1, 5)$       426)  $(-1, -8)$   
 428)  $(6, -3)$       429) No solution.  
 432)  $(9, 2), (9, -10), (8, -2), (8, -6)$   
 434)  $(6, -4), (-10, -4), (6, 9), (-10, 9)$   
 437)  $(-6, 5)$       438)  $(-2, -4)$   
 440)  $(-1, -6)$       441)  $(-3, -6)$   
 443)  $(7, 10), (7, 2), (2, 10), (2, 2)$   
 445)  $(7, 0)$       446)  $(0, 2), (5, -9), (-5, -9)$       447)  $(-6, 1)$   
 448)  $(-5, 7), (-7, 7)$       449)  $(-5, -2), (-5, -8), (0, -3), (0, -7)$       450) No solution.  
 451)  $(6, 5), (-8, 5)$       452)  $(-2, 0), (-10, 0)$   
 454)  $(2, -2), (5, 6), (5, -10)$       455) 22      456) 26  
 457) 10      458) 19      459) 42      460) 23  
 461) 32      462) 14      463) 19      464) 29  
 465) 7      466) 48      467) 26      468) 11  
 469) 26      470) 64      471) 9      472) 9  
 473) 19      474) 48      475)  $\frac{39}{2} = 19.5$       476)  $\frac{43}{2} = 21.5$   
 477) 56      478)  $\frac{13}{2} = 6.5$       479)  $\frac{13}{2} = 6.5$       480) 31  
 481) 22      482)  $\frac{21}{2} = 10.5$       483)  $\frac{39}{2} = 19.5$       484)  $\frac{17}{2} = 8.5$   
 485)  $16 \cdot \sum_{k=1}^n k^2 + 8 \cdot \sum_{k=1}^n 1$   
 $16 \cdot \frac{n(n+1)(2n+1)}{6} + 8n$   
 $\frac{16n^3}{3} + 8n^2 + \frac{32n}{3}$   
 486)  $36 \cdot \sum_{k=1}^n k + 30 \cdot \sum_{k=1}^n 1$   
 $36 \cdot \frac{n(n+1)}{2} + 30n$   
 $18n^2 + 48n$   
 487)  $27 \cdot \sum_{k=1}^n k^2 + 15 \cdot \sum_{k=1}^n 1$   
 $27 \cdot \frac{n(n+1)(2n+1)}{6} + 15n$   
 $9n^3 + \frac{27n^2}{2} + \frac{39n}{2}$   
 488)  $9 \cdot \sum_{k=1}^n k + 15 \cdot \sum_{k=1}^n 1$   
 $9 \cdot \frac{n(n+1)}{2} + 15n$   
 $\frac{39n}{2} + \frac{9n^2}{2}$   
 489)  $16 \cdot \sum_{k=1}^n k^2 + 10 \cdot \sum_{k=1}^n 1$   
 $16 \cdot \frac{n(n+1)(2n+1)}{6} + 10n$   
 $\frac{16n^3}{3} + 8n^2 + \frac{38n}{3}$   
 490)  $27 \cdot \sum_{k=1}^n k^2 + 6 \cdot \sum_{k=1}^n 1$   
 $27 \cdot \frac{n(n+1)(2n+1)}{6} + 6n$   
 $9n^3 + \frac{27n^2}{2} + \frac{21n}{2}$   
 491)  $8 \cdot \sum_{k=1}^n k^2 + 12 \cdot \sum_{k=1}^n 1$   
 $8 \cdot \frac{n(n+1)(2n+1)}{6} + 12n$   
 $\frac{8n^3}{3} + 4n^2 + \frac{40n}{3}$   
 492)  $8 \cdot \sum_{k=1}^n k^2 + 10 \cdot \sum_{k=1}^n 1$   
 $8 \cdot \frac{n(n+1)(2n+1)}{6} + 10n$   
 $\frac{8n^3}{3} + 4n^2 + \frac{34n}{3}$   
 493)  $3 \cdot \sum_{k=1}^n k + 4 \cdot \sum_{k=1}^n 1$   
 $3 \cdot \frac{n(n+1)}{2} + 4n$   
 $\frac{11n}{2} + \frac{3n^2}{2}$

494)  $27 \cdot \sum_{k=1}^n k + 9 \cdot \sum_{k=1}^n 1$   
 $27 \cdot \frac{n(n+1)}{2} + 9n$   
 $\frac{45n}{2} + \frac{27n^2}{2}$

$18$   
496)  $\lim_{n \rightarrow \infty} \left( \frac{1}{n} \cdot \sum_{k=1}^n 1 + \frac{2}{n^3} \cdot \sum_{k=1}^n k^2 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{1}{n} \cdot n + \frac{2}{n^3} \cdot \frac{n(n+1)(2n+1)}{6} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{5}{3} + \frac{1}{n} + \frac{1}{3n^2} \right)$   
 $\frac{5}{3} \approx 1.667$

498)  $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot \sum_{k=1}^n 1 + \frac{2}{n^3} \cdot \sum_{k=1}^n k^2 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot n + \frac{2}{n^3} \cdot \frac{n(n+1)(2n+1)}{6} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{20}{3} + \frac{1}{n} + \frac{1}{3n^2} \right)$   
 $\frac{20}{3} \approx 6.667$

500)  $\lim_{n \rightarrow \infty} \left( \frac{4}{n} \cdot \sum_{k=1}^n 1 + \frac{48}{n^2} \cdot \sum_{k=1}^n k \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{4}{n} \cdot n + \frac{48}{n^2} \cdot \frac{n(n+1)}{2} \right)$   
 $\lim_{n \rightarrow \infty} \left( 28 + \frac{24}{n} \right)$   
 $28$

502)  $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot \sum_{k=1}^n 1 + \frac{72}{n^2} \cdot \sum_{k=1}^n k \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot n + \frac{72}{n^2} \cdot \frac{n(n+1)}{2} \right)$   
 $\lim_{n \rightarrow \infty} \left( 42 + \frac{36}{n} \right)$   
 $42$

495)  $\lim_{n \rightarrow \infty} \left( \frac{9}{n} \cdot \sum_{k=1}^n 1 + \frac{27}{n^3} \cdot \sum_{k=1}^n k^2 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{9}{n} \cdot n + \frac{27}{n^3} \cdot \frac{n(n+1)(2n+1)}{6} \right)$   
 $\lim_{n \rightarrow \infty} \left( 18 + \frac{27}{2n} + \frac{9}{2n^2} \right)$

18

497)  $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot \sum_{k=1}^n 1 + \frac{2}{n^2} \cdot \sum_{k=1}^n k \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot n + \frac{2}{n^2} \cdot \frac{n(n+1)}{2} \right)$   
 $\lim_{n \rightarrow \infty} \left( 7 + \frac{1}{n} \right)$   
 $7$

499)  $\lim_{n \rightarrow \infty} \left( \frac{9}{n} \cdot \sum_{k=1}^n 1 + \frac{27}{n^2} \cdot \sum_{k=1}^n k \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{9}{n} \cdot n + \frac{27}{n^2} \cdot \frac{n(n+1)}{2} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{45}{2} + \frac{27}{2n} \right)$   
 $\frac{45}{2} = 22.5$

501)  $\lim_{n \rightarrow \infty} \left( \frac{3}{n} \cdot \sum_{k=1}^n 1 + \frac{2}{n^3} \cdot \sum_{k=1}^n k^2 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{3}{n} \cdot n + \frac{2}{n^3} \cdot \frac{n(n+1)(2n+1)}{6} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{11}{3} + \frac{1}{n} + \frac{1}{3n^2} \right)$   
 $\frac{11}{3} \approx 3.667$

503)  $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot \sum_{k=1}^n 1 + \frac{4}{n^2} \cdot \sum_{k=1}^n k \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot n + \frac{4}{n^2} \cdot \frac{n(n+1)}{2} \right)$   
 $\lim_{n \rightarrow \infty} \left( 8 + \frac{2}{n} \right)$   
 $8$

504)  $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot \sum_{k=1}^n 1 + \frac{1}{n^2} \cdot \sum_{k=1}^n k \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot n + \frac{1}{n^2} \cdot \frac{n(n+1)}{2} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{13}{2} + \frac{1}{2n} \right)$   
 $\frac{13}{2} = 6.5$

505)  $\lim_{n \rightarrow \infty} \left( \frac{8}{n} \cdot \sum_{k=1}^n 1 + \frac{16}{n^3} \cdot \sum_{k=1}^n k^2 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{8}{n} \cdot n + \frac{16}{n^3} \cdot \frac{n(n+1)(2n+1)}{6} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{40}{3} + \frac{8}{n} + \frac{8}{3n^2} \right)$   
 $\frac{40}{3} \approx 13.333$

507)  $\lim_{n \rightarrow \infty} \left( \frac{4}{n} \cdot \sum_{k=1}^n 1 + \frac{16}{n^3} \cdot \sum_{k=1}^n k^2 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{4}{n} \cdot n + \frac{16}{n^3} \cdot \frac{n(n+1)(2n+1)}{6} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{28}{3} + \frac{8}{n} + \frac{8}{3n^2} \right)$   
 $\frac{28}{3} \approx 9.333$

509)  $\lim_{n \rightarrow \infty} \left( \frac{12}{n} \cdot \sum_{k=1}^n 1 + \frac{8}{n^3} \cdot \sum_{k=1}^n k^2 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{12}{n} \cdot n + \frac{8}{n^3} \cdot \frac{n(n+1)(2n+1)}{6} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{44}{3} + \frac{4}{n} + \frac{4}{3n^2} \right)$   
 $\frac{44}{3} \approx 14.667$

511)  $\lim_{n \rightarrow \infty} \left( \frac{12}{n} \cdot \sum_{k=1}^n 1 + \frac{16}{n^4} \cdot \sum_{k=1}^n k^3 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{12}{n} \cdot n + \frac{16}{n^4} \cdot \frac{n^2 \cdot (n+1)^2}{4} \right)$   
 $\lim_{n \rightarrow \infty} \left( 16 + \frac{8}{n} + \frac{4}{n^2} \right)$   
 $16$

513)  $\lim_{n \rightarrow \infty} \left( \frac{1}{n} \cdot \sum_{k=1}^n 1 + \frac{1}{n^4} \cdot \sum_{k=1}^n k^3 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{1}{n} \cdot n + \frac{1}{n^4} \cdot \frac{n^2 \cdot (n+1)^2}{4} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{5}{4} + \frac{1}{2n} + \frac{1}{4n^2} \right)$   
 $\frac{5}{4} = 1.25$

515)  $-\frac{65}{6} \approx -10.833$       516)  $\frac{20}{3} \approx 6.667$   
519)  $-\frac{26}{3} \approx -8.667$       520)  $\frac{16}{3} \approx 5.333$   
523) 9      524)  $\frac{21}{4} = 5.25$

506)  $\lim_{n \rightarrow \infty} \left( \frac{1}{n} \cdot \sum_{k=1}^n 1 + \frac{1}{n^3} \cdot \sum_{k=1}^n k^2 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{1}{n} \cdot n + \frac{1}{n^3} \cdot \frac{n(n+1)(2n+1)}{6} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{4}{3} + \frac{1}{2n} + \frac{1}{6n^2} \right)$   
 $\frac{4}{3} \approx 1.333$

508)  $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot \sum_{k=1}^n 1 + \frac{1}{n^4} \cdot \sum_{k=1}^n k^3 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{6}{n} \cdot n + \frac{1}{n^4} \cdot \frac{n^2 \cdot (n+1)^2}{4} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{25}{4} + \frac{1}{2n} + \frac{1}{4n^2} \right)$   
 $\frac{25}{4} = 6.25$

510)  $\lim_{n \rightarrow \infty} \left( \frac{2}{n} \cdot \sum_{k=1}^n 1 + \frac{16}{n^3} \cdot \sum_{k=1}^n k^2 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{2}{n} \cdot n + \frac{16}{n^3} \cdot \frac{n(n+1)(2n+1)}{6} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{22}{3} + \frac{8}{n} + \frac{8}{3n^2} \right)$   
 $\frac{22}{3} \approx 7.333$

512)  $\lim_{n \rightarrow \infty} \left( \frac{2}{n} \cdot \sum_{k=1}^n 1 + \frac{16}{n^4} \cdot \sum_{k=1}^n k^3 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{2}{n} \cdot n + \frac{16}{n^4} \cdot \frac{n^2 \cdot (n+1)^2}{4} \right)$   
 $\lim_{n \rightarrow \infty} \left( 6 + \frac{8}{n} + \frac{4}{n^2} \right)$   
 $6$

514)  $\lim_{n \rightarrow \infty} \left( \frac{3}{n} \cdot \sum_{k=1}^n 1 + \frac{1}{n^3} \cdot \sum_{k=1}^n k^2 \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{3}{n} \cdot n + \frac{1}{n^3} \cdot \frac{n(n+1)(2n+1)}{6} \right)$   
 $\lim_{n \rightarrow \infty} \left( \frac{10}{3} + \frac{1}{2n} + \frac{1}{6n^2} \right)$   
 $\frac{10}{3} \approx 3.333$

517) 12      518)  $\frac{35}{6} \approx 5.833$   
521)  $-\frac{35}{6} \approx -5.833$       522)  $-\frac{11}{3} \approx -3.667$   
525)  $\frac{-e+1}{e} \approx -0.632$       526)  $\frac{-3e+3}{e} \approx -1.896$

$$527) \frac{12}{5} = 2.4$$

$$531) \frac{9\sqrt[3]{3} - 3}{2} \approx 4.99$$

$$534) 8$$

$$538) \frac{6 - 2\sqrt{3}}{3} \approx 0.845$$

$$542) -2$$

$$545) \frac{49}{6} \approx 8.167$$

$$549) \frac{-6 + 4\sqrt{3}}{3} \approx 0.309$$

$$552) -\frac{15\sqrt[3]{2}}{4} \approx -4.725$$

$$555) \int_6^{15} \frac{2}{u^2} du$$

$$559) \int_{-3}^0 -3u^2 du$$

$$563) \int_6^3 -\frac{2}{u^2} du$$

$$567) 3$$

$$571) \frac{9}{7} \approx 1.286$$

$$575) -\frac{3}{5} = -0.6$$

$$579) \frac{2}{5} = 0.4$$

$$583) -\frac{9}{10} = -0.9$$

$$586) \int_3^6 \frac{3}{x} dx$$

$$589) \int_{-4}^{-1} \frac{1}{x^2} dx$$

$$592) \int_{-5}^0 \left( \frac{x^2}{2} + 3x + \frac{11}{2} \right) dx$$

$$595) \int_{-1}^3 \left( \frac{x^2}{2} + 2x + 2 \right) dx$$

$$= \frac{62}{3} \approx 20.667$$

$$528) \frac{2e^3 - 2}{e^2} \approx 5.166$$

$$532) -\frac{3}{5} = -0.6$$

$$535) \frac{3e^3 - 3}{e^3} \approx 2.851$$

$$539) -15$$

$$543) \frac{-2e^3 + 2}{e^2} \approx -5.166$$

$$546) \frac{4}{3} \approx 1.333$$

$$550) \frac{2}{3} \approx 0.667$$

$$553) -\ln 2 + \ln 6 \approx 1.099$$

$$556) \int_{10}^4 \frac{2}{u^2} du$$

$$560) \int_{-1}^0 3u^3 du$$

$$564) \int_{20}^4 -\frac{2}{u^2} du$$

$$568) -\frac{6}{7} \approx -0.857$$

$$572) \frac{2}{5} = 0.4$$

$$576) -\frac{6}{5} = -1.2$$

$$580) 20$$

$$584) \frac{2}{3} \approx 0.667$$

$$587) \int_{-5}^{-2} \left( \frac{x^2}{2} + x + \frac{1}{2} \right) dx$$

$$590) \int_4^7 \frac{5}{x} dx$$

$$593) \int_1^5 \frac{3}{x} dx$$

$$596) \int_{-7}^{-2} -\frac{3}{x} dx$$

$$= -3 \ln 2 + 3 \ln 7 \approx 3.758$$

$$529) -\frac{71}{30} \approx -2.367$$

$$533) \frac{27\sqrt[3]{3} - 54\sqrt[3]{6}}{4} \approx -14.796$$

$$536) \frac{1}{24} \approx 0.042$$

$$540) -\frac{9}{2} = -4.5$$

$$544) \frac{5 \ln 8 - 5 \ln 2}{2} \approx 3.466$$

$$547) \frac{3 + \sqrt{3}}{3} \approx 1.577$$

$$551) -11$$

$$554) 2 \ln 3 \approx 2.197$$

$$557) \int_2^6 -\frac{1}{u^2} du$$

$$561) \int_5^2 -\frac{2}{u^2} du$$

$$565) -\frac{3}{10} = -0.3$$

$$569) -\frac{3}{5} = -0.6$$

$$573) -\frac{3}{10} = -0.3$$

$$577) \frac{1}{4} = 0.25$$

$$581) -\frac{3}{10} = -0.3$$

$$585) \int_{-6}^{-2} \left( \frac{x^2}{2} + 2x + 4 \right) dx$$

$$588) \int_1^3 \frac{1}{x^2} dx$$

$$591) \int_2^4 \frac{3}{x^2} dx$$

$$594) \int_2^6 \sqrt{x} dx$$

$$597) \int_4^5 \sqrt{x} dx$$

$$530) \frac{20}{9} \approx 2.222$$

$$537) \frac{\pi}{12} \approx 0.262$$

$$541) -32$$

$$548) -27$$

$$558) \int_{20}^4 -\frac{2}{u^2} du$$

$$562) \int_3^7 -\frac{3}{u^2} du$$

$$566) \frac{3}{7} \approx 0.429$$

$$570) \frac{3}{10} = 0.3$$

$$574) \frac{1}{4} = 0.25$$

$$578) -\frac{9}{10} = -0.9$$

$$582) \frac{4}{5} = 0.8$$

$$= \frac{2(5\sqrt{5} - 8)}{3} \approx 2.12$$

$$598) \int_1^2 \frac{1}{x^2} dx \\ = \frac{1}{2} = 0.5$$

$$599) \int_2^4 \frac{5}{x} dx \\ = 5 \ln 4 - 5 \ln 2 \approx 3.466$$

$$600) \int_{-5}^{-2} (x^2 + 4x + 6) dx \\ = 15$$

$$601) \int_3^7 \frac{3}{x} dx \\ = 3 \ln 7 - 3 \ln 3 \approx 2.542$$

$$602) \int_1^3 \frac{3}{x^2} dx \\ = 2$$

$$603) \int_3^7 \sqrt{x} dx \\ = \frac{2(-3\sqrt{3} + 7\sqrt{7})}{3} \approx 8.883$$

$$604) \int_0^4 (x^2 - 4x + 5) dx \\ = \frac{28}{3} \approx 9.333$$

$$605) \int_{\frac{2\pi}{3}}^{\pi} 2\sin x dx \\ = 1$$

$$606) \int_{\frac{\pi}{2}}^{\frac{2\pi}{3}} \sin x dx \\ = \frac{1}{2} = 0.5$$

$$607) \int_{-\pi}^{-\frac{5\pi}{6}} \sec^2 x dx \\ = \frac{\sqrt{3}}{3} \approx 0.577$$

$$608) \int_{\frac{\pi}{3}}^{\frac{\pi}{2}} \sin x dx \\ = \frac{1}{2} = 0.5$$

$$609) \int_0^{\frac{\pi}{6}} \cos x dx \\ = \frac{1}{2} = 0.5$$

$$610) \int_{-\frac{\pi}{3}}^{-\frac{\pi}{4}} 2\csc x \cot x dx \\ = \frac{2(3\sqrt{2} - 2\sqrt{3})}{3} \approx 0.519$$

$$611) \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} \csc x \cot x dx \\ = -1 + \sqrt{2} \approx 0.414$$

$$612) \int_{\frac{\pi}{6}}^{\frac{2\pi}{3}} \sin x dx \\ = \frac{1 + \sqrt{3}}{2} \approx 1.366$$

$$613) \int_{-\frac{3\pi}{4}}^{-\frac{\pi}{2}} -2\cos x dx \\ = 2 - \sqrt{2} \approx 0.586$$

$$614) \int_{\frac{\pi}{3}}^{\pi} \sin x dx \\ = \frac{3}{2} = 1.5$$

$$615) \int_{-4}^{-1} (-x^2 - 6x - 9 - (x - 3)) dx \\ = \frac{27}{2} = 13.5$$

$$616) \int_1^3 \left( \frac{1}{x^2} + 3 \right) dx \\ = \frac{20}{3} \approx 6.667$$

$$617) \int_{-3}^{-1} \left( \frac{3}{x^2} + 1 \right) dx \\ = 4$$

$$618) \int_{-5}^{-2} \left( x^2 + 8x + 12 - \left( \frac{x^2}{2} + 4x + 3 \right) \right) dx \\ = \frac{9}{2} = 4.5$$

$$619) \int_{-3}^{-2} \left( \frac{1}{x^2} + 3 \right) dx \\ = \frac{19}{6} \approx 3.167$$

$$620) \int_{-3}^0 \left( -\frac{x}{2} + 3 + \frac{x^2}{2} \right) dx \\ = \frac{63}{4} = 15.75$$

$$621) \int_1^4 \left( 4 - \frac{4}{x^2} \right) dx \\ = 9$$

$$622) \int_0^4 (\sqrt{x} + 3\sqrt{x}) dx \\ = \frac{64}{3} \approx 21.333$$

$$623) \int_{-3}^{-1} \left( \frac{4}{x^2} + 3 \right) dx \\ = \frac{26}{3} \approx 8.667$$

$$625) \int_{-6}^{-4} \left( \frac{x^2}{2} + 2x \right) dx + \\ \int_{-4}^{-2} \left( -4 - \left( \frac{x^2}{2} + 2x - 4 \right) \right) dx \\ = 8$$

$$627) \int_{-3}^{-1} \left( \frac{x^2}{2} + 1 - \left( \frac{x^2}{2} + 4x + 5 \right) \right) dx + \\ \int_{-1}^0 \left( \frac{x^2}{2} + 4x + 5 - \left( \frac{x^2}{2} + 1 \right) \right) dx \\ = 10$$

$$629) \int_{-4}^{-3} \left( -x^2 - 8x - 11 - (-2x^2 - 8x - 2) \right) dx + \\ \int_{-3}^{-2} \left( -2x^2 - 8x - 2 - (-x^2 - 8x - 11) \right) dx \\ = 6$$

$$631) \int_1^3 \left( x^2 - 6x + 10 - \left( \frac{x^2}{2} - x - \frac{1}{2} \right) \right) dx + \\ \int_3^5 \left( \frac{x^2}{2} - x - \frac{1}{2} - (x^2 - 6x + 10) \right) dx \\ = 8$$

$$633) \int_{-3}^{-2} \left( x^2 + 2x - (-x^2 + 4) \right) dx + \\ \int_{-2}^1 \left( -x^2 + 4 - (x^2 + 2x) \right) dx \\ = \frac{38}{3} \approx 12.667$$

$$635) \int_{-3}^0 \left( -x - (-x^3 - x^2 + 5x) \right) dx + \\ \int_0^2 \left( -x^3 - x^2 + 5x + x \right) dx \\ = \frac{253}{12} \approx 21.083$$

$$624) \int_0^1 \left( x^2 - 2x + 3 + 2x^2 \right) dx \\ = 3$$

$$626) \int_{-4}^0 \left( -\frac{x^2}{2} - 2x - 2 - (x^2 + 4x - 2) \right) dx + \\ \int_0^1 \left( x^2 + 4x - 2 - \left( -\frac{x^2}{2} - 2x - 2 \right) \right) dx \\ = \frac{39}{2} = 19.5$$

$$628) \int_{-5}^{-4} (x^2 + 4x) dx + \\ \int_{-4}^{-2} (1 - (x^2 + 4x + 1)) dx \\ = \frac{23}{3} \approx 7.667$$

$$630) \int_{-5}^{-1} \left( -x^2 - 6x - 4 - (x^2 + 6x + 6) \right) dx + \\ \int_{-1}^0 \left( x^2 + 6x + 6 - (-x^2 - 6x - 4) \right) dx \\ = 26$$

$$632) \int_{-3}^{-1} \left( -x - 2 - (x^2 + 6x + 4) \right) dx + \\ \int_{-1}^0 \left( x^2 + 6x + 4 - (-x - 2) \right) dx \\ = \frac{61}{6} \approx 10.167$$

$$634) \int_{-5}^{-2} \left( -2x - 4 - (x^2 + 6x + 8) \right) dx + \\ \int_{-2}^{-1} \left( x^2 + 6x + 8 - (-2x - 4) \right) dx \\ = \frac{34}{3} \approx 11.333$$

$$636) \int_{-2}^0 (x^3 - 4x) dx + \\ \int_0^2 (x^2 - (x^3 + x^2 - 4x)) dx \\ = 8$$

$$637) \int_{-2}^0 \left( -\frac{x^2}{2} - \left( -\frac{x^3}{2} + 3x \right) \right) dx + \\ \int_0^3 \left( -\frac{x^3}{2} + 3x + \frac{x^2}{2} \right) dx \\ = \frac{253}{24} \approx 10.542$$

$$639) \int_{-3}^0 \left( \frac{x^3}{2} + \frac{x^2}{2} - 3x \right) dx + \\ \int_0^2 \left( x - \left( \frac{x^3}{2} + \frac{x^2}{2} - 2x \right) \right) dx \\ = \frac{253}{24} \approx 10.542$$

$$641) \int_{-2}^0 \left( -\frac{x^2}{2} - \left( -\frac{x^3}{2} - \frac{x^2}{2} + 2x \right) \right) dx + \\ \int_0^2 \left( -\frac{x^3}{2} - \frac{x^2}{2} + 2x + \frac{x^2}{2} \right) dx \\ = 4$$

$$643) \int_0^3 \left( -x^2 + 4x - (-x^3 + 7x^2 - 11x) \right) dx + \\ \int_3^5 \left( -x^3 + 7x^2 - 11x - (-x^2 + 4x) \right) dx \\ = \frac{253}{12} \approx 21.083$$

$$645) 2 \int_{-4}^4 \left( 4 - \frac{x^2}{4} \right)^2 dx \\ = \frac{2048}{15} \approx 136.533$$

$$648) 2 \int_{-4}^4 \left( -\frac{x^2}{4} + 4 \right)^2 dx \\ = \frac{2048}{15} \approx 136.533$$

$$651) \frac{1}{2} \int_{-2}^2 (-x^2 + 4)^2 dx \\ = \frac{256}{15} \approx 17.067$$

$$654) \frac{1}{2} \int_{-3}^3 \left( 1 - \frac{x^2}{9} \right)^2 dx \\ = \frac{8}{5} = 1.6$$

$$638) \int_{-3}^0 \left( -\frac{x^3}{2} - \frac{x^2}{2} + 3x \right) dx + \\ \int_0^2 \left( -\frac{x^3}{2} - \frac{x^2}{2} + 3x - 0 \right) dx \\ = \frac{253}{24} \approx 10.542$$

$$640) \int_0^2 \left( -x^2 + 4x - \left( -\frac{x^3}{2} + 2x^2 \right) \right) dx + \\ \int_2^4 \left( -\frac{x^3}{2} + 2x^2 - (-x^2 + 4x) \right) dx \\ = 4$$

$$642) \int_{-2}^0 (2x^3 + 2x^2 - 4x) dx + \\ \int_0^1 (x^2 - (2x^3 + 3x^2 - 4x)) dx \\ = \frac{37}{6} \approx 6.167$$

$$644) \int_{-2}^0 \left( \frac{x^3}{2} - x^2 - 4x \right) dx + \\ \int_0^4 \left( x - \left( \frac{x^3}{2} - x^2 - 3x \right) \right) dx \\ = \frac{74}{3} \approx 24.667$$

$$646) 2 \int_{-7}^7 (\sqrt{49 - x^2})^2 dx \\ = \frac{2744}{3} \approx 914.667$$

$$647) \int_{-5}^5 (\sqrt{25 - x^2})^2 dx \\ = \frac{500}{3} \approx 166.667$$

$$649) \int_{-2}^2 (-x^2 + 4)^2 dx \\ = \frac{512}{15} \approx 34.133$$

$$650) \int_{-3}^3 \left( 1 - \frac{x^2}{9} \right)^2 dx \\ = \frac{16}{5} = 3.2$$

$$652) \int_{-4}^4 (\sqrt{16 - x^2})^2 dx \\ = \frac{256}{3} \approx 85.333$$

$$653) \int_{-1}^1 (1 - x^2)^2 dx \\ = \frac{16}{15} \approx 1.067$$

$$655) \frac{\sqrt{3}}{4} \int_{-5}^5 \left( \sqrt{9 - \frac{9x^2}{25}} + \sqrt{9 - \frac{9x^2}{25}} \right)^2 dx \\ = 60\sqrt{3} \approx 103.923$$

$$656) \frac{1}{4} \int_{-7}^7 (\sqrt{49 - x^2})^2 dx \\ = \frac{343}{3} \approx 114.333$$

$$657) \frac{\sqrt{3}}{4} \int_{-7}^7 (\sqrt{49 - x^2})^2 dx \\ = \frac{343\sqrt{3}}{3} \approx 198.031$$

$$658) \frac{1}{2} \int_{-2}^2 (4 - x^2)^2 dx \\ = \frac{256}{15} \approx 17.067$$

$$659) \frac{\pi}{8} \int_{-7}^7 \left( \sqrt{4 - \frac{4x^2}{49}} + \sqrt{4 - \frac{4x^2}{49}} \right)^2 dx \\ = \frac{56\pi}{3} \approx 58.643$$

$$660) \frac{\sqrt{3}}{4} \int_{-7}^7 (\sqrt{49 - x^2} + \sqrt{49 - x^2})^2 dx \\ = \frac{1372\sqrt{3}}{3} \approx 792.125$$

$$661) \frac{1}{4} \int_{-3}^3 (\sqrt{9 - x^2})^2 dx \\ = 9$$

$$662) \frac{1}{2} \int_{-5}^5 (\sqrt{25 - x^2})^2 dx \\ = \frac{250}{3} \approx 83.333$$

$$663) \frac{1}{4} \int_{-2}^2 (-x^2 + 4)^2 dx \\ = \frac{128}{15} \approx 8.533$$

$$664) \frac{1}{2} \int_{-2}^2 \left( \sqrt{49 - \frac{49x^2}{4}} + \sqrt{49 - \frac{49x^2}{4}} \right)^2 dx \\ = \frac{784}{3} \approx 261.333$$

$$665) \frac{1}{2} \int_0^7 (\sqrt{49 - y^2} + \sqrt{49 - y^2})^2 dy \\ = \frac{1372}{3} \approx 457.333$$

$$666) \frac{\sqrt{3}}{4} \int_0^6 (\sqrt{36 - y^2} + \sqrt{36 - y^2})^2 dy \\ = 144\sqrt{3} \approx 249.415$$

$$667) \frac{\pi}{8} \int_0^7 (\sqrt{49 - y^2} + \sqrt{49 - y^2})^2 dy \\ = \frac{343\pi}{3} \approx 359.189$$

$$668) \frac{1}{4} \int_{-6}^6 \left( \sqrt{16 - \frac{16y^2}{36}} + \sqrt{16 - \frac{16y^2}{36}} \right)^2 dy \\ = 128$$

$$669) \frac{\pi}{8} \int_{-7}^7 \left( \sqrt{16 - \frac{16y^2}{49}} + \sqrt{16 - \frac{16y^2}{49}} \right)^2 dy \\ = \frac{224\pi}{3} \approx 234.572$$

$$670) \frac{\pi}{8} \int_{-7}^7 \left( \sqrt{36 - \frac{36y^2}{49}} + \sqrt{36 - \frac{36y^2}{49}} \right)^2 dy \\ = 168\pi \approx 527.788$$

$$671) \frac{1}{4} \int_{-7}^7 \left( \sqrt{16 - \frac{16y^2}{49}} + \sqrt{16 - \frac{16y^2}{49}} \right)^2 dy \\ = \frac{448}{3} \approx 149.333$$

$$672) \frac{1}{4} \int_{-7}^7 \left( \sqrt{25 - \frac{25y^2}{49}} + \sqrt{25 - \frac{25y^2}{49}} \right)^2 dy \\ = \frac{700}{3} \approx 233.333$$

$$673) \frac{1}{2} \int_{-5}^5 \left( \sqrt{16 - \frac{16y^2}{25}} + \sqrt{16 - \frac{16y^2}{25}} \right)^2 dy \\ = \frac{640}{3} \approx 213.333$$

$$674) \frac{1}{2} \int_{-6}^6 \left( \sqrt{9 - \frac{9y^2}{36}} + \sqrt{9 - \frac{9y^2}{36}} \right)^2 dy \\ = 144$$

$$675) \pi \int_4^6 (\sqrt{x+2})^2 dx \quad 676) \pi \int_0^1 (x^2)^2 dx \\ = 14\pi \approx 43.982 \quad = \frac{1}{5}\pi \approx 0.628$$

$$677) \pi \int_0^4 (\sqrt{x})^2 dx \\ = 8\pi \approx 25.133$$

$$678) \pi \int_{-3}^0 (2\sqrt{x+5})^2 dx \\ = 42\pi \approx 131.947$$

$$679) \pi \int_0^1 (\sqrt[3]{x})^2 dx \\ = \frac{3}{5}\pi \approx 1.885$$

$$680) \pi \int_1^7 (2\sqrt{x+1})^2 dx \\ = 120\pi \approx 376.991$$

$$681) \pi \int_0^1 (\sqrt{x})^2 dx \\ = \frac{1}{2}\pi \approx 1.571$$

$$682) \pi \int_{-1}^1 (-x^2 + 1)^2 dx \\ = \frac{16}{15}\pi \approx 3.351$$

$$683) \pi \int_{-2}^2 (-x^2 + 4)^2 dx \\ = \frac{512}{15}\pi \approx 107.233$$

$$684) \pi \int_0^1 (-x^2 + 1)^2 dx \\ = \frac{8}{15}\pi \approx 1.676$$

$$685) \pi \int_{-2}^2 (-y^2 + 4)^2 dy \\ = \frac{512}{15}\pi \approx 107.233$$

$$686) \pi \int_0^1 (y^3)^2 dy \\ = \frac{1}{7}\pi \approx 0.449$$

$$687) \pi \int_0^4 (\sqrt{y})^2 dy \\ = 8\pi \approx 25.133$$

$$688) \pi \int_0^1 (y^2)^2 dy \\ = \frac{1}{5}\pi \approx 0.628$$

$$689) \pi \int_{-1}^1 (-y^2 + 1)^2 dy \\ = \frac{16}{15}\pi \approx 3.351$$

$$690) \pi \int_0^1 (-y^2 + 1)^2 dy \\ = \frac{8}{15}\pi \approx 1.676$$

$$691) \pi \int_0^1 (\sqrt{y})^2 dy \\ = \frac{1}{2}\pi \approx 1.571$$

$$692) \pi \int_0^2 (y^2)^2 dy \\ = \frac{32}{5}\pi \approx 20.106$$

$$693) \pi \int_0^2 (-y^2 + 4)^2 dy \\ = \frac{256}{15}\pi \approx 53.617$$

$$694) \pi \int_0^1 ((-x^2 + 2)^2 - 1) dx \\ = \frac{28}{15}\pi \approx 5.864$$

$$695) \pi \int_{-2}^0 ((x^2 + 4)^2 - 3^2) dx \\ = \frac{626}{15}\pi \approx 131.109$$

$$696) \pi \int_1^4 (6^2 - (\sqrt{x})^2) dx \\ = \frac{201}{2}\pi \approx 315.73$$

$$697) \pi \int_0^1 ((\sqrt{x} + 3)^2 - (x^2 + 3)^2) dx \\ = \frac{23}{10}\pi \approx 7.226$$

$$698) \pi \int_{-1}^1 ((-x^2 + 3)^2 - 2^2) dx \\ = \frac{32}{5}\pi \approx 20.106$$

$$699) \pi \int_{-1}^1 ((-x^2 + 2)^2 - 1) dx \\ = \frac{56}{15}\pi \approx 11.729$$

$$700) \pi \int_1^4 (5^2 - (\sqrt{x})^2) dx \\ = \frac{135}{2}\pi \approx 212.058$$

$$701) \pi \int_0^1 ((\sqrt{x} + 4)^2 - (x^2 + 4)^2) dx \\ = \frac{89}{30}\pi \approx 9.32$$

$$702) \pi \int_1^4 (4^2 - (\sqrt{x})^2) dx \\ = \frac{81}{2}\pi \approx 127.235$$

$$703) \pi \int_0^4 ((\sqrt{x} + 3)^2 - 3^2) dx \\ = 40\pi \approx 125.664$$

$$704) \pi \int_{\frac{1}{4}}^2 \left(4^2 - \left(\frac{1}{y}\right)^2\right) dy \\ = \frac{49}{2}\pi \approx 76.969$$

$$705) \pi \int_0^1 ((\sqrt{y} + 1)^2 - 1) dy \\ = \frac{11}{6}\pi \approx 5.76$$

$$706) \pi \int_0^1 (1 - (y^3)^2) dy \\ = \frac{6}{7}\pi \approx 2.693$$

$$707) \pi \int_0^4 ((\sqrt{y} + 1)^2 - 1) dy \\ = \frac{56}{3}\pi \approx 58.643$$

$$708) \pi \int_0^1 ((-y^2 + 2)^2 - 1) dy \\ = \frac{28}{15}\pi \approx 5.864$$

- 709)  $\pi \int_{-2}^2 ((-y^2 + 6)^2 - 2^2) dy$   
 $= \frac{384}{5}\pi \approx 241.274$
- 710)  $\pi \int_{-2}^2 ((-y^2 + 5)^2 - 1) dy$   
 $= \frac{832}{15}\pi \approx 174.254$
- 711)  $\pi \int_0^1 ((\sqrt{y} + 3)^2 - 3^2) dy$   
 $= \frac{9}{2}\pi \approx 14.137$
- 712)  $\pi \int_0^4 ((\sqrt{y} + 3)^2 - 3^2) dy$   
 $= 40\pi \approx 125.664$
- 713)  $\pi \int_0^2 ((-y^2 + 5)^2 - 1) dy$   
 $= \frac{416}{15}\pi \approx 87.127$
- 714)  $\pi \int_0^2 ((2x)^2 - (x^2)^2) dx$   
 $= \frac{64}{15}\pi \approx 13.404$
- 715)  $\pi \int_{-2}^2 ((-x^2 + 5)^2 - 1) dx$   
 $= \frac{832}{15}\pi \approx 174.254$
- 716)  $\pi \int_0^1 ((3 - x^2)^2 - (3 - \sqrt{x})^2) dx$   
 $= \frac{17}{10}\pi \approx 5.341$
- 717)  $\pi \int_0^4 ((\sqrt{x} + 1)^2 - 1) dx$   
 $= \frac{56}{3}\pi \approx 58.643$
- 718)  $\pi \int_{-1}^2 ((x^2 + 2)^2 - 1) dx$   
 $= \frac{138}{5}\pi \approx 86.708$
- 719)  $\pi \int_0^1 (3^2 - (3 - \sqrt{x})^2) dx$   
 $= \frac{7}{2}\pi \approx 10.996$
- 720)  $\pi \int_0^1 ((x^2 + 1)^2 - 1) dx$   
 $= \frac{13}{15}\pi \approx 2.723$
- 721)  $\pi \int_0^1 ((\sqrt{x} + 4)^2 - 4^2) dx$   
 $= \frac{35}{6}\pi \approx 18.326$
- 722)  $\pi \int_0^1 ((\sqrt{x} + 1)^2 - 1) dx$   
 $= \frac{11}{6}\pi \approx 5.76$
- 723)  $\pi \int_0^2 ((x^2 + 1)^2 - 1) dx$   
 $= \frac{176}{15}\pi \approx 36.861$
- 724)  $\pi \int_{-1}^1 ((-y^2 + 3)^2 - 2^2) dy$   
 $= \frac{32}{5}\pi \approx 20.106$
- 725)  $\pi \int_0^2 ((-y^2 + 5)^2 - 1) dy$   
 $= \frac{416}{15}\pi \approx 87.127$
- 726)  $\pi \int_0^4 ((\sqrt{y} + 3)^2 - \left(\frac{y}{2} + 3\right)^2) dy$   
 $= \frac{32}{3}\pi \approx 33.51$
- 727)  $\pi \int_0^2 ((-y^2 + 6)^2 - 2^2) dy$   
 $= \frac{192}{5}\pi \approx 120.637$
- 728)  $\pi \int_0^1 (5^2 - (5 - \sqrt{y})^2) dy$   
 $= \frac{37}{6}\pi \approx 19.373$
- 729)  $\pi \int_0^4 ((\sqrt{y} + 1)^2 - \left(\frac{y}{2} + 1\right)^2) dy$   
 $= \frac{16}{3}\pi \approx 16.755$
- 730)  $\pi \int_0^4 ((\sqrt{y} + 3)^2 - 3^2) dy$   
 $= 40\pi \approx 125.664$
- 731)  $\pi \int_0^1 ((\sqrt{y} + 3)^2 - (y^2 + 3)^2) dy$   
 $= \frac{23}{10}\pi \approx 7.226$
- 732)  $\pi \int_0^1 ((\sqrt{y} + 2)^2 - (y^2 + 2)^2) dy$   
 $= \frac{49}{30}\pi \approx 5.131$
- 733)  $\pi \int_0^1 ((\sqrt{y} + 1)^2 - 1) dy$   
 $= \frac{11}{6}\pi \approx 5.76$

$$734) \quad 2\pi \int_0^1 x(-x^2 + 3 - 2) dx \\ = \frac{1}{2}\pi$$

$$735) \quad 2\pi \int_{\frac{1}{4}}^5 x\left(4 - \frac{1}{x}\right) dx \\ = \frac{361}{4}\pi$$

$$736) \quad 2\pi \int_2^{\frac{5}{2}} x\left(5 - \frac{2}{x}\right) dx \\ = \frac{169}{5}\pi$$

$$737) \quad 2\pi \int_0^1 x(x^2 + 2 - 2) dx \\ = \frac{1}{2}\pi$$

$$738) \quad 2\pi \int_0^1 x(1 - \sqrt[3]{x}) dx \\ = \frac{1}{7}\pi$$

$$739) \quad 2\pi \int_0^1 x(5 - \sqrt{x}) dx \\ = \frac{21}{5}\pi$$

$$740) \quad 2\pi \int_0^2 x(2x + 1 - (x^2 + 1)) dx \\ = \frac{8}{3}\pi$$

$$741) \quad 2\pi \int_1^4 x(6 - \sqrt{x}) dx \\ = \frac{326}{5}\pi$$

$$742) \quad 2\pi \int_0^2 x(-x^2 + 6 - (-x + 4)) dx \\ = \frac{16}{3}\pi$$

$$743) \quad 2\pi \int_0^2 x(-x^2 + 6 - 2) dx \\ = 8\pi$$

$$744) \quad 2\pi \int_{\frac{1}{3}}^5 y\left(3 - \frac{1}{y}\right) dy \\ = \frac{196}{3}\pi$$

$$745) \quad 2\pi \int_0^1 y(\sqrt{y} + 1 - 1) dy \\ = \frac{4}{5}\pi$$

$$746) \quad 2\pi \int_0^1 y(1 - y^3) dy \\ = \frac{3}{5}\pi$$

$$747) \quad 2\pi \int_0^1 y(\sqrt{y} + 3 - (y^2 + 3)) dy \\ = \frac{3}{10}\pi$$

$$748) \quad 2\pi \int_0^4 y(\sqrt{y} + 3 - 3) dy \\ = \frac{128}{5}\pi$$

$$749) \quad 2\pi \int_0^2 y(-y^2 + 5 - 1) dy \\ = 8\pi$$

$$750) \quad 2\pi \int_0^1 y(y^2 + 1 - 1) dy \\ = \frac{1}{2}\pi$$

$$751) \quad 2\pi \int_0^1 y(-y^2 + 3 - 2) dy \\ = \frac{1}{2}\pi$$

$$752) \quad 2\pi \int_0^1 y \cdot y^3 dy \\ = \frac{2}{5}\pi$$

$$753) \quad 2\pi \int_0^4 y\left(\sqrt{y} + 3 - \left(3 + \frac{y}{2}\right)\right) dy \\ = \frac{64}{15}\pi$$

$$754) \quad 2\pi \int_0^1 (1-x)(\sqrt{x} + 1 - (x^2 + 1)) dx \\ = \frac{11}{30}\pi$$

$$755) \quad 2\pi \int_0^1 (1-x)(\sqrt{x} + 4 - 4) dx \\ = \frac{8}{15}\pi$$

$$756) \quad 2\pi \int_0^1 (1-x)(-x^2 + 5 - (x+3)) dx \\ = \frac{3}{2}\pi$$

$$757) \quad 2\pi \int_0^1 (x+4)(1 - \sqrt[3]{x}) dx \\ = \frac{15}{7}\pi$$

$$758) \quad 2\pi \int_0^2 (3-x)(2x+2-(x^2+2)) dx \\ = \frac{16}{3}\pi$$

$$760) \quad 2\pi \int_0^2 (2-x)(-x^2+4-(-x+2)) dx \\ = 8\pi$$

$$762) \quad 2\pi \int_{-1}^1 (5-x)(-x^2+7-(x^2+5)) dx \\ = \frac{80}{3}\pi$$

$$764) \quad 2\pi \int_0^1 (3-y)y^3 dy \quad 765) \quad 2\pi \int_0^1 (y+3)(1-y^3) dy \\ = \frac{11}{10}\pi \quad = \frac{51}{10}\pi$$

$$766) \quad 2\pi \int_0^1 (3-y)(-y^2+3-2) dy \\ = \frac{7}{2}\pi$$

$$768) \quad 2\pi \int_0^1 (2-y)(y^2+1-1) dy \quad 769) \quad 2\pi \int_0^1 (y+3)y^3 dy \\ = \frac{5}{6}\pi \quad = \frac{19}{10}\pi$$

$$770) \quad 2\pi \int_0^4 (y+1)(\sqrt{y}+2-2) dy \\ = \frac{544}{15}\pi$$

$$772) \quad 2\pi \int_0^1 (y+1)y^3 dy \quad 773) \quad 2\pi \int_0^2 (y+3)(-y^2+6-2) dy \\ = \frac{9}{10}\pi \quad = 40\pi$$

$$775) \quad y = \frac{1}{x-3} - 1, x < 3$$

$$778) \quad y = -\cos x$$

$$781) \quad y = 2\ln(-x+1) - 3, x < 1$$

$$784) \quad y = 3\cos x - 2$$

$$787) \quad y = -2\ln x, x > 0$$

$$759) \quad 2\pi \int_0^4 (x+4)(\sqrt{x}+4-4) dx \\ = \frac{1024}{15}\pi$$

$$761) \quad 2\pi \int_0^1 (2-x)(\sqrt{x}+4-4) dx \\ = \frac{28}{15}\pi$$

$$763) \quad 2\pi \int_0^2 (5-x)(2x-x^2) dx \\ = \frac{32}{3}\pi$$

$$767) \quad 2\pi \int_0^4 (2-y)(\sqrt{y}+3-3) dy \\ = \frac{64}{15}\pi$$

$$771) \quad 2\pi \int_0^1 (3-y)(y^2+1-1) dy \\ = \frac{3}{2}\pi$$

$$774) \quad y = 2\ln -x, x < 0$$

$$776) \quad y = 2\ln -x - 1, x < 0$$

$$777) \quad y = \cos x - 1$$

$$780) \quad y = \frac{2}{3x^3}, x > 0$$

$$782) \quad y = \frac{2}{x-2}, x < 2$$

$$783) \quad y = \frac{1}{x+3} - 3, x > -3$$

$$785) \quad y = -\frac{1}{x+1} + 1, x > -1$$

$$786) \quad y = \cos x - 1$$

$$788) \quad y = 2\sin x - 3$$

$$789) \quad y = -\frac{1}{x} + 2, x > 0$$

$$790) \quad y = -\frac{1}{x+1} + 3, \quad x > -1$$

$$793) \quad y = -\frac{1}{x+1} + 1, \quad x > -1$$

$$796) \quad \frac{y^3}{3} = \frac{x^4}{2} + C_1 \\ y = \sqrt[3]{\frac{3x^4}{2} + C}$$

$$800) \quad \tan y = x + C \\ y = \tan^{-1}(x + C)$$

$$791) \quad y = -\frac{1}{3x^3} + 3, \quad x > 0$$

$$794) \quad \frac{y^3}{3} = x^2 + C_1 \\ y = \sqrt[3]{3x^2 + C}$$

$$797) \quad \frac{e^{2y}}{2} = x^2 + C_1 \\ y = \frac{\ln(2x^2 + C)}{2}$$

$$801) \quad \sin y = x + C \\ y = \sin^{-1}(x + C)$$

$$792) \quad y = -\cos x$$

$$795) \quad \frac{y^3}{3} = e^x + C_1 \\ y = \sqrt[3]{3e^x + C}$$

$$798) \quad \cos y = x + C \\ y = \cos^{-1}(x + C)$$

$$799) \quad \frac{y^3}{3} = 2e^x + C_1 \\ y = \sqrt[3]{6e^x + C}$$

$$802) \quad e^y = 3e^x + C \\ y = \ln(3e^x + C)$$

$$803) \quad \frac{y^3}{3} = x^2 + C_1 \\ y = \sqrt[3]{3x^2 + C}$$